

# **Comparison of Transmission Loss Allocation Methods and Prediction of Losses in Deregulated Power Systems**

by

MATEMEKE EDWINAH MAREDI

DISSERTATION

Submitted to the  
Electrical and Electronics Engineering Programme  
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in partial fulfilment of the requirement for the  
BACHELOR OF ENGINEERING (Hons)  
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UNIVERSITI TEKNOLOGI PETRONAS  
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December 2010

## **CERTIFICATION OF APPROVAL**

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Univesiti Teknologi PETRONAS

Tronoh, Perak

December 2010

## **CERTIFICATION OF ORIGINALITY**

This is to certify that I am responsible for the work submitted in this project, that the original work is my own except as specified in the references and acknowledgements, and that the original work contained herein have not been undertaken or done by unspecified sources or persons.

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MATEMEKE EDWINAH MAREDI

## **ABSTRACT**

Transmission losses are a significant component of the amount of power to be generated in order to meet the power demand. Today, in competitive electric energy markets operating under pool-based, bilateral contracts or hybrid model, transmission losses must be allocated among the market participants. This process should take to account the buyer and seller spatial locations on the network as well as the non-linear interaction among simultaneous transactions in order to reflect the real market operation and adequate economic efficiencies. In this paper, four methods for transmission loss allocation in power systems operating in a deregulated competitive environment are discussed and compared. Losses for oncoming operations are then predicted. Test results using the IEEE 24-bus RTS are presented. Relevant conclusions, comments and suggestions are also included.

## **ACKNOWLEDGEMENT**

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# **CHAPTER 1**

## **INTRODUCTION**

### **1.1 Background of Study**

In many countries, electricity industries are being restructured and liberalized. Electricity is now a commodity, bought and sold by generators, retailers (suppliers) and other traders. Vertically integrated utilities are being broken up, which allows end-users and distributors to buy power from more distant generators.

Deregulation of electricity is the process by which the government removes or reduces the restrictions of the electricity industry. The electric utility is no longer under the control of one organization. The main aim of deregulation is to improve competition among the electricity retailers, which improves the efficiency of the industry and electricity pricing.

In a deregulated market, there are several retailers using the same transmission company. This poses a problem of having to distribute the losses that occur during transmission and distribution in a fair manner among the retailers. This is where transmission loss allocation comes in. Transmission loss allocation deals with the allocation of transmission losses among the retailers.

There are various methods for transmission loss allocation. Various methods for loss allocation will be studied and compared to study the advantages and disadvantages of these methods. The methods to be researched include pro rata, incremental loss, unsubsidized incremental, proportional sharing method.

## 1.2 Problem statement

The introduction of deregulation into the electricity market has changed many aspects of the industry. The reform required reorganization and rethinking of the traditional issues of power balance, stability, security and economy. Previously vertically integrated industry comprising of generation, transmission and distribution sectors had been decomposed into separate independent entities. New market structures were introduced in which markets are modeled by either pool, bilateral contracts, or a combination of both called the hybrid [1]. These deregulated markets are governed by System Operators that monitor the daily operation of the market, as well as ensuring a secure operation and facilitating an economical operation.

The pricing of electricity has always been a major concern to system participants, even before the introduction of deregulation. The previous monopolistic structure used a simple pricing scheme based on a uniform distribution of the approximated loss of 2 % to 5 % of generated power. This simple loss allocation, however, is not sufficient for the restructured electricity market as it does not encourage competition between market participants. Given that healthy competition should encourage lower prices, it is important to develop an electricity-pricing scheme that promotes competition.

To promote fair competition, market participants must be charged in a way that reflects their use of the system. A critical part of this is the distribution of system losses to the market participants.

Even though there are different methods for loss allocation, they all allocate losses in different ways. The choice of a method depends on the desired results and the system settings.

There is sometimes also a problem of the power supply not meeting the

demand, so to avoid power failures and such problems, it's important for the suppliers to know how much the demand is. That's where prediction of oncoming operations is of importance.

### **1.3. Objectives**

- To do a study of deregulated systems.
- To do research and study various methods of loss allocation.
- Compare the methods to see the differences and similarities.
- Do qualitative and quantitative measurements to see which method produces better results.
- Predict transmission losses for oncoming operating scenarios.

### **1.4 Scope of Study**

This project involves detailed research on transmission loss allocation in deregulated systems. There will be journals reviewed based on transmission loss allocation in various settings.

Various methods for loss allocation will be looked into and discussed in detail to do a comparison.

Prediction of transmission losses in a transaction for oncoming scenarios will also be performed.

## CHAPTER 2

### LITERATURE REVIEW

#### 2.1 Deregulation

Electricity markets around the world are undergoing major changes to improve the economic efficiency and effectiveness of electricity supply. To promote competition, previously vertically integrated utilities have been broken up into separate generation, transmission and retailing companies. In addition, open electricity markets have been formed to facilitate the trading of electricity.

An electric system, as illustrated in figure 1, consist of three main parts; generation, transmission and distribution.

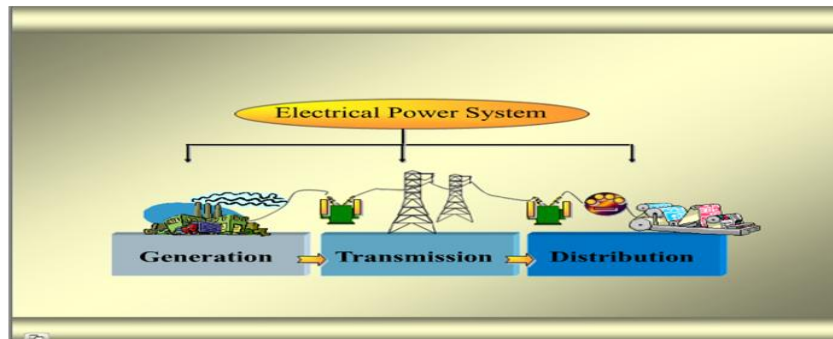


Figure 1: A regulated electric system

In a regulated system, the generation, transmission and distribution are the responsibility of a single organization. Figure 2 illustrates,

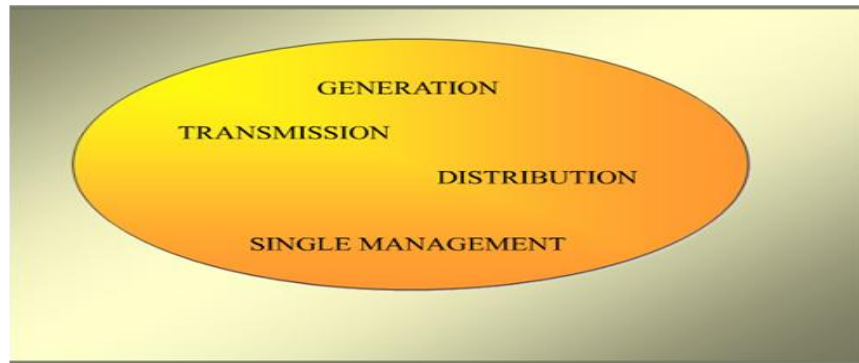


Figure 2: An illustration of a regulated system

In a deregulated structure however, a transmission system is being used by multiple generation and distribution companies that do not own the transmission system, as illustrates in figure 3.

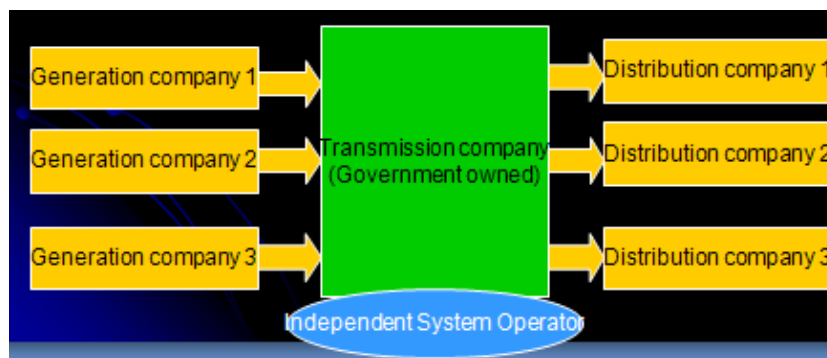


Figure 3: An illustration of a deregulated system

In view of the operation of deregulated systems, it becomes more important to know the role of individual generators and loads to transmission wires and power transfer between individual generators to loads. Under restructuring and deregulation, vertically integrated utilities, which producers generate, transmit and distribute electricity, have been functionally unbundled. Deregulation introduces competition in the wholesale generation and retailing of electricity.

With separate pricing of generation, transmission and distribution, it is necessary to find the capacity usage of different transactions happening at the

same time so that fair usage-of-transmission-system charge can be given to individual customer separately. That way, transparency in a deregulated system can be achieved. Capacity usage is an important issue for transmission; therefore, the power produced by each generator and consumed by each load should be traced. In these aspects, problems arise because all transactions have to share the same transmission network simultaneously.

Those problems include

- Which generators are supplying this load?
- Which generator or load is making the biggest use of the transmission line?
- Which generator or load is producing loss of this transmission line?

need to have acceptable solutions in a fair deregulated system [1].

## **2.2 Loss allocation methods**

To solve the problem of loss allocation in a deregulated system, an algorithm, which can allocate the contributions of power flow and loss from individual generator through the transmission system to the loads, is needed. More sophisticated treatment of losses, in contrast to traditional methods that arbitrarily assign losses as 2 % to 5 % of generated power, is critical in overcoming this problem [2]. Essentially, the loss allocation chosen is a part of the design of the market itself.

A carefully selected loss allocation method must be able to do the following:

- promote efficient matching of supply and demand;
- provide indicative measures for location advantages of market participants; and
- provide information on the need and appropriate location of network expansions.

It is crucial for market operators of the deregulated market to adopt loss allocation methods that are compatible with their market structures, as well as promoting competition between market participants. Different markets globally have employed different loss allocation schemes, no loss allocation method has been universally accepted. In Australia the National Electricity Market (NEM), which is managed by the National Electricity Market Management Company (NEMMCO) has used a form of approximated marginal loss allocation [3]. In contrast, the Great Britain, Spain and Brazil market has employed the simpler pro rata method [4]. Furthermore, New Zealand has adopted the full marginal loss allocation method [5].

The fact that not a single method of loss allocation can be universally accepted suggests that there are deficiencies in all current methods, leading to continued research in this field. Some methods are so unsatisfactory that some markets, such as Brazil, to consider implementing alternative approaches [6].

Among some of the currently used methods for loss allocation are pro rata, marginal, proportional sharing, loss formula, and circuit theory based [7].

We will review four of these methods, namely, pro rata, proportional sharing, incremental transmission loss (ITL) and unsubsidized incremental transmission loss (U-ITL).

### ***2.2.1. Pro rata method***

The simplest method is the pro rata method, which is based on an arbitrary division of losses between active generation and load.

First, losses are globally assigned to generators and consumers, for instance 50 % of losses are allocated to each category. Then, a proportional



allocation rule is used: the losses allocated to a generator (consumer) are proportional to its corresponding level of energy generation (consumption). A PR procedure is currently used in the electricity market of mainland Spain where 100 % of losses are allocated to consumers [8].

The advantage of pro rata procedures are simple to understand and implement. The disadvantage of this method is that it does not take account of the geographic distribution of the network. It “ignores” the network. That is, two identical demands located respectively near generating buses and far away from these buses are equally treated, and this is unfair for the load located near the generating buses [9].

### ***2.2.2 Marginal Procedures (ITL) and Unsubsidized ITL***

Loss allocation using the incremental method is fundamentally simple, being based on the concept of numerical integration. However, the incremental results depend on the formulation of the marginal-loss function which is, in turn, governed by how the system evolves to a current state through incremental power changes [10]. In all existing methods, the marginal-loss functions are derived using certain user-defined and arbitrary criteria to maintain the load-generation balance for small power changes. These criteria may or may not reflect the actual performance of the system. As such, the resulting allocations are at best theoretical and can have little practical application for costing purposes.

Losses are assigned to generators and demands through the so-called incremental transmission loss (ITL) coefficients [11]. Normalization is performed after the assignment because this allocation procedure typically results in over-recovery. The standard marginal procedure based on ITL coefficients depends on the selection of the slack bus because ITL coefficients do

depend on the slack bus. The ITL coefficient of the slack bus is zero by definition, thus the slack bus is allocated no losses. This is a drastic limitation for this method that requires that pool agents agree beforehand on the selection of the slack bus. Furthermore, ITL coefficients can be either positive or negative which may result in the allocation of negative losses to certain buses. The unsubsidized marginal allocation (U-ITL) can be used to get rid of these negative losses.

### ***2.2.3 Proportional sharing procedure (PS)***

The use of the results of a converged power flow plus a linear proportional sharing principle [12] makes it possible for the allocation of losses to generators and consumers. This principle states that the power flow reaching a bus from any power line splits among the lines evacuating power from the bus proportionally to their corresponding power flows, which is neither provable nor disprovable.

Proportional sharing procedures, on top of electrical laws, require the assumption of the proportional sharing principle. Using this principle, losses are allocated by linear procedures. To allocate losses to demands, the method relies on a simple principle: losses associated with every line whose flow enters a given bus are transferred to the lines whose flows leave the bus (or demands in that bus) proportionally to the flows of those lines (the flows of which leave the bus). It should be noted that a systematic application of this principle originates that all losses are allocated to demands. Analogously, in order to allocate losses to generators, the method relies on a simple principle: losses associated with every line whose flow leaves a given bus are transferred to the lines whose flows enter the bus (or generations in that bus) proportionally to the flows of those lines (whose flows enter the bus). It should be noted that a systematic application of this principle originates that all losses are allocated to generators. The sole

information required to apply this method is the real power flow and the losses in every line, and the power generated or consumed in every bus.

Due to the fact that no unique or ideal procedure exists, any loss allocation algorithm should have most of the desirable properties stated below:

- to be consistent with the results of a power flow
- to depend on the amount of energy either produced or consumed
- to depend on the relative location in the transmission network
- to avoid volatility
- to provide appropriate economic marginal signals
- to be easy to understand
- to be simple to implement

### **2.3 Prediction of Losses in a Transaction**

A generalized quadratic relationship can be used to learn the relationships between a retailer's demand and the line losses in each line used by a transaction, by generating learning coefficients [13]. The current operating scenario and a few past operating scenarios related to a specific transaction can be used to generate the coefficients. Using the generated learning coefficients, power loss for a transaction for any oncoming operating scenario can be determined.

These relationships exist as long as the network configuration remains unchanged and the voltages at the retailing points are restored close to their original values. These relationships, for a specific network configuration, can be learned through learning coefficients and these learning coefficients can be used to determine the corresponding power loss for a transaction.

## 2.4 Power flow tracing

In [14], Bialek presents a power flow tracing method that can be used for transmission loss allocation. The method may be applied to both real and reactive power flows. The method allows assessment of how much of the real and reactive power output from a particular station goes to a particular load. It also allows the assessment of contributions of individual generators or loads to individual line flows. A loss partitioning algorithm has also been introduced which allows the break down of the total transmission loss into components to be allocated to individual loads or generators.

The mesh structure of high-voltage transmission networks provides a large number of possible routes by which electrical power can flow from the source (generators) to the sinks (loads). Tracing the connections using the load flow program is not possible as changing demand or generation at any node would result in a corresponding change of generation coming from the marginal plant. Hence, the conventional wisdom is that with an integrated system, it is not possible to trace electricity from a particular generator to a particular supplier.

It is only possible to determine relation between the generators (or loads) and the flows of in transmission lines by means of sensitivity analysis, that is by determining how a change in a nodal generation/demand influences the flow in a particular line.

The method of tracing is of particular interest especially in deregulated systems. In this context, the problem of tracing gains importance as its solution could enhance the transparency in the operation of the transmission system. An electricity tracing method will make it possible to charge the suppliers and/or generators for the actual amount of losses caused and hence encourage

efficiency. Whether or not a generator or supplier should be penalized for its graphical location is not considered in this case.

The tracing method used here is topological in nature; it deals with a general transportation problem of how the flows are distributed in a meshed network. For the tracing method used in [13], the network is assumed to be connected and described by a set of  $n$  nodes,  $m$  directed links (transmission lines or transformers),  $2m$  flows (at both ends of each link) and a number of sources (generators) and sinks (loads) connected to the nodes. Practically the only requirement for the input data is that Kirchhoffs Current Law must be satisfied for all the nodes in the network. In this respect the method is equally applicable to real and reactive power flows and direct currents. Neglecting the Kirchhoff s Voltage Law does not introduce any further errors as the law has been already used to obtain the flows.

The main principle used to trace the flow of electricity will be that of proportional sharing [13]. This is illustrated in figure 1 where four lines are connected to node  $i$ , two with inflows and two with outflows. The total power flow through the node is  $P_i = 40 + 60 = 100\text{MW}$  of which 40% is supplied by line  $j-i$  and 60% by line  $k-i$ . As electricity is indistinguishable and each of the outflows down the line from node  $i$  is dependent only on the voltage gradient and impedance of the line, it may be assumed that each MW leaving the node contains the same proportion of the inflows as the total nodal flow  $P_i$ . Hence the 70MW outflowing in line  $i-m$  consists of  $70 \times 40 / 100 = 28\text{MW}$  supplied by line  $j-i$  and  $70 \times 60 / 100 = 42\text{MW}$  supplied by line  $k-i$ . Similarly the 30MW outflowing in line  $i-l$  consists of  $30 \times 40 / 100 = 12\text{MW}$  supplied by line  $j-i$  and  $30 \times 60 / 100 = 18\text{MW}$  supplied by line  $k-i$ .

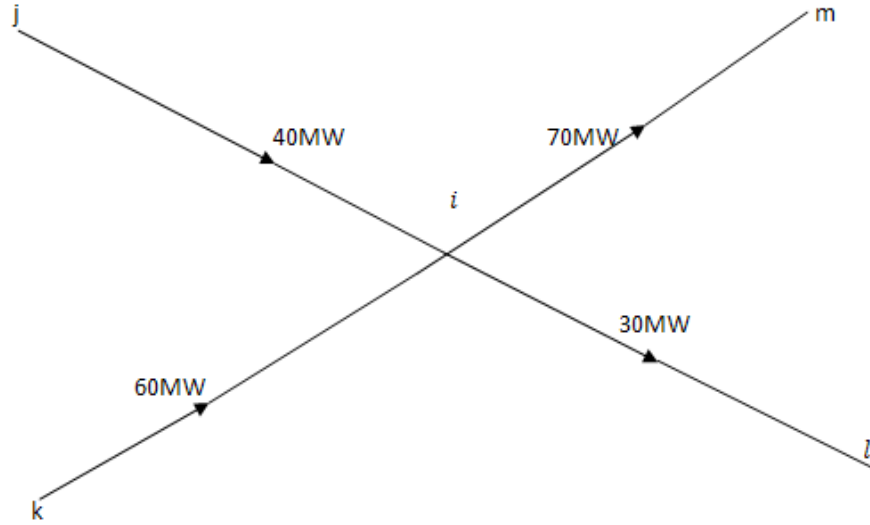


Figure 4: Proportional sharing principle

The proportional sharing principle basically amounts to assuming that the network node is a perfect ‘mixer’ of incoming flows so that it is impossible to tell which particular inflowing electron goes into which particular outgoing line. This seems to agree with common sense and with the generally accepted view that electricity is indistinguishable. As it is impossible to ‘dye’ the incoming flows and check the color of the outflows, the proportional sharing principle can be neither proved nor disproved. This, however, is irrelevant as the principle will be applied here for nontechnical calculations. In this respect, the principle is fair as it treats all the incoming and outflowing flows in the same way. In other words, no particular generator or load is distinguished in any way.

Tracing electricity can be seen as a transportation problem of determining how the power injected by generators is distributed between the lines and loads of the network. The algorithm proposed works only on lossless flows when the flows at the beginning and end of each line are the same. In the simplest way of obtaining lossless flows from the lossy ones is by assuming that a line flow is an average over the sending- and receiving-end flows and by adding half of the line loss to the power injections at each terminal node of the line.

Consider for example a simple system shown in Figure 2 with active and reactive power flows obtained from AC load flow program. A number on top or to the left of the line indicates a real power flow, while a number below or to the right of the line indicates a reactive power flow. A similar convention has been used for the generators and the loads. The total transmission loss in the network is equal to the sum of all the line losses and equals  $(225 - 218) + (83 - 82) + (173 - 171) + (60 - 59) + (115 - 112) = 14\text{MW}$ .

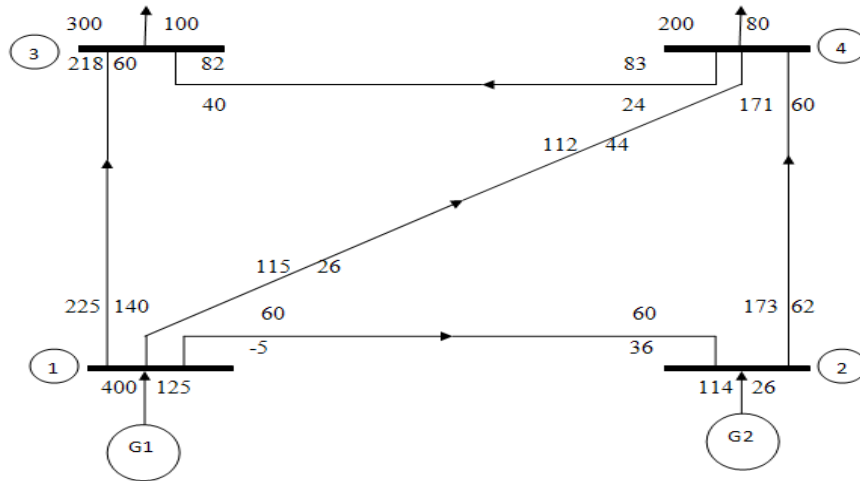


Figure 5: AC power flow in four node network

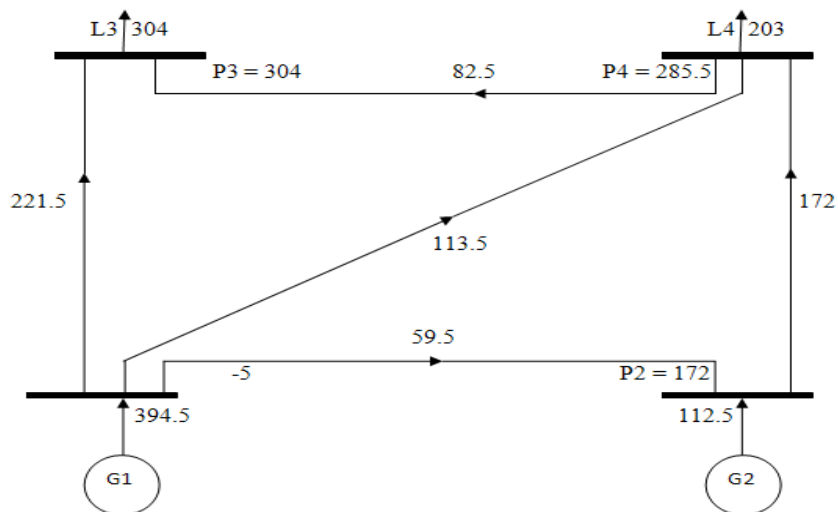


Figure 6: Lossless power flow

Figure 3 shows a lossless real power flow obtained from the lossy flow of figure 2.

The algorithm for tracing the flow of electricity will be now derived in two versions. The downstream-looking algorithm will look at the nodal balance of outflows while the dual, upstream-looking algorithm, will look at the nodal balance of inflows [13]. The upstream-looking algorithm will apportion the losses to the loads and allocate the supplement charge to the generators. The downstream-looking algorithm will apportion the losses to the generators and allocate the supplement charge to the loads.

#### ***Upstream-looking algorithm***

Assume that it is possible to break down the total transmission loss into components to be added to individual load demands. The sum of the actual demand of a particular load plus the allocated part of the total transmission loss is referred to as the gross demand. Obviously the total system gross demand is equal to the total actual generation.

#### ***Downstream-looking algorithm***

The downstream-looking algorithm allocates the supplement charge to individual loads. The transmission loss is dealt with by breaking it down into components to be subtracted from individual generators. The actual generation of a particular generator minus the allocated part of the total transmission loss will be referred to as the net generation.

One of the possible applications of the electricity tracing method lies in the apportioning of the transmission loss to individual generators or loads in the



network. This can be done by accumulating the losses as the power flows to individual loads (or from individual generators). The nodal loss is assumed to be shared between nodal outflows proportionally to the square (or any other power) of the outflows. The loss allocation does not depend on the choice of the marginal generator and always results in positive charges. This algorithm requires solving a sparse linear equation of the rank equal to the number of network nodes.

It is envisaged that the proposed method could have wide applications in the deregulated electricity supply industry. Apart from giving additional insight into how power flows in the network, it can be used to set tariffs for transmission services based on the shared, as opposed to marginal, costs. This includes charging for the transmission loss and for the actual usage of the system by a particular generator or the load. The method can also be used to assess the contribution of individual sources of reactive power in satisfying individual reactive power demands and therefore be used as a tool for reactive power pricing

## CHAPTER 3

### METHODOLOGY

#### 3.1 Procedure Identification

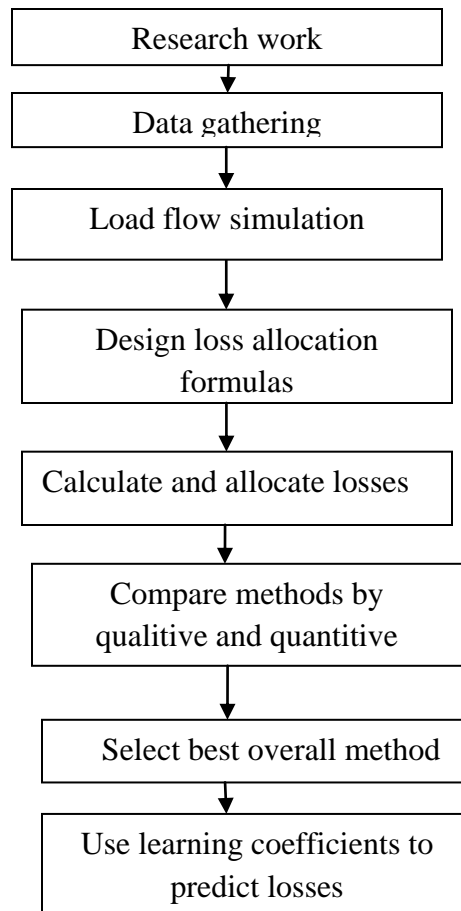


Figure 7: Flow chart of the project

#### 3.2 Tools and equipment required

- Matlab
- Matpower

### 3.3 Applied method

First, note that the sum of all generations is equal to the sum of all demands plus the losses. That is

$$P_G = P_D + L, P_G = \sum_{i=1}^{N_G} P_{Gi}, P_D = \sum_{j=1}^{N_D} P_{Dj} \quad (1)$$

where

$P_G$	=	total active power generated;
$P_{Gi}$	=	power output of generators of bus;
$P_D$	=	total active power demand;
$P_{Dj}$	=	active power demanded by consumers of bus j;
$L$	=	transmission power losses;
$N_G$	=	number of generating buses;
$N_D$	=	number of demand buses.

For simplicity and without loss of generality, it is assumed that in every bus there are at most one generator and one demand. Therefore, no distinction will be made henceforth between generator, load, and bus.

The considered transmission loss allocation methods are described in the four subsections below [10].

#### 3.3.1 Pro Rata Allocation (PR)

The PR method proportionally allocates 50% of losses to the demands and 50% to the generators, that is

$$L_{Gi} = \frac{L}{2} \frac{P_{Gi}}{P_G}, \quad L_{Di} = \frac{L}{2} \frac{P_{Di}}{P_D} \quad (2)$$

where  $L_{Gi}$  is the losses allocated to the generator  $i$ ,  $L_{Dj}$  and are the losses allocated to the demand  $j$ . Generation and demand loss allocation factors are computed, respectively, as

$$L_{Gi} = \frac{1}{2} \frac{P_{Gi}}{P_G} = K_G P_{Gi}, \quad K_G = \frac{1}{2} \frac{L}{P_G} \quad (3)$$

$$L_{Di} = \frac{1}{2} \frac{P_{Di}}{P_D} = K_D P_{Di}, \quad K_D = \frac{1}{2} \frac{L}{P_D} \quad (4)$$

It should be noted that generation loss allocation factors  $K_G$  are identical for all buses, and demand loss allocation factors  $K_D$  are also identical for all buses. Additionally, it should be noted that losses allocated to generators and demands are always positive.

### 3.3.2 Marginal Allocation (ITL)

This method uses ITL coefficients to proportionally allocate losses to generators and demands. ITLs are easily obtained from a converged power flow [15]. The ITL of a given bus provides the change in total losses produced by an incremental change in the power injected in that bus. Therefore

$$K_i = \frac{\partial L}{\partial (P_{Gi} - P_{Di})} \quad (5)$$

where  $K_i$  is the ITL corresponding to bus  $i$ . It should be noted that the ITL of the slack bus is zero by definition.

First computations of the losses allocated to generator  $i$  and demand  $j$  are, respectively,

$$L_{Gi} = P_{Gi} \frac{\partial L}{\partial P_{Gi}} = P_{Gi} K_i \quad (6)$$

$$L_{Di} = P_{Di} \frac{\partial L}{\partial P_{Dj}} = -P_{Di} K_j \quad (7)$$

However as a result of nonlinearities, the sum of these allocated losses ( $L'$ ) does not match total actual (measured) losses  $L$ . Therefore, a normalization procedure is used to allocate the exact amount of losses  $L$ , that is

$$L \neq \sum_{i=1}^{N_G} L_{Gi} + \sum_{j=1}^{N_D} L_{Dj} = \sum_{i=1}^{N_G} P_{Gi} K_i - \sum_{j=1}^{N_D} P_{Dj} K_j = L' \quad (8)$$

Therefore a normalization procedure is used to allocate the exact amount of losses  $L$

$$\begin{aligned} L &= L' \frac{L}{L'} = \left( \sum_{i=1}^{N_G} P_{Gi} K_i - \sum_{j=1}^{N_D} P_{Dj} K_j \right) \frac{L}{L'} \\ &= \sum_{i=1}^{N_G} P_{Gi} K'_i - \sum_{j=1}^{N_D} P_{Dj} K'_j \end{aligned} \quad (9)$$

where  $K'_i = K_i(L/L')$  is the normalized ITL coefficient for bus  $i$ .

Finally, losses allocated to every generator and demands are, respectively,

$$L'_{Gi} = P_{Gi} K'_i \quad L'_{Dj} = -P_{Dj} K'_j \quad (10)$$

It should be noted that this marginal procedure may allocate negative losses to either generators or demands, and these negative losses can be interpreted as cross subsidies [10].

### 3.3.2 Unsubsidized Marginal Allocation (U-ITL)

The unsubsidized ITL (U-ITL) method modifies in a consistent manner ITL coefficients so that negative losses are avoided. A set of ITLs is defined for

generators and a different one for demands. The purpose of this method is to actually allocate the cost of losses, not to explain physical facts.

ITL coefficients, computed for a given slack bus, can easily be referred to a different slack bus by defining a translation coefficient  $\beta$  ( $0 \leq \beta \leq 1$ ) [10].

Total losses can be computed as

$$L = \sum_{i=1}^N K_i' P_i \quad (11)$$

where

$N$  number of buses;

$K_i'$  normalized ITL coefficient of bus ;

$P_i$  injected active power in bus  $i$  ( $P_i = P_{Gi} - P_{Di}$ ).

Total losses can also be expressed as

$$L = \sum_{i=1}^N (P_{Gi} - P_{Di}) = \sum_{i=1}^N P_i \quad (12)$$

Multiplying (11) by  $\beta$  ( $0 \leq \beta \leq 1$ ) and (12) by  $1 - \beta$ , and adding both, total losses can be expressed as

$$L = \sum_{i=1}^N \beta K_i' P_i + \sum_{i=1}^N (1 - \beta) P_i \quad (13)$$

which results in

$$L = \sum_{i=1}^N [\beta K_i' + (1 - \beta)] P_i = \sum_{i=1}^N K_i P_i \quad (14)$$

where  $\beta K_i' + (1 - \beta)$  constitutes a new ITL coefficient  $K_i = \beta K_i' + (1 - \beta)$ .

In respect to the generation, a change of slack bus is performed in such a way that the generator ITL coefficient with smallest value becomes zero. This makes it impossible to assign negative losses to generators. This is accomplished as stated below.

Let  $K'_{Gk}$  be the normalized generation ITL coefficient with the smallest value, the translation coefficient  $\beta_G$  is then computed as

$$K_{Gk} = 0 = \beta_G K'_{Gk} + (1 - \beta_G) \quad (15)$$

and

$$\beta_G = \frac{1}{1 - K'_{Gk}}$$

The new ITL coefficients for generators can be expressed as

$$K_{Gi} = \beta_G K'_{Gk} + (1 - \beta_G). \quad (16)$$

Those coefficients are again normalized to allocate 50% of losses to generators.

In respect to demands, the translation coefficient  $\beta_D$  is computed from

$$K_{Dm} = 0 = \beta_D K'_{Dm} + (1 - \beta_D) \quad (17)$$

where  $K'_{Dm}$  is the demand ITL coefficient with the highest value. Equation (17) guarantees that no demand gets allocated negative losses. Therefore, demand ITL coefficients become all negative.

From (17),  $\beta_D = 1/(1 - K'_{Dm})$ .

The new demand ITL coefficients become

$$K_{Dj} = \beta_D K'_{Dj} + (1 - \beta_D). \quad (18)$$

### 3.3.4 Proportional Sharing Allocation (PS)

This algorithm is a brief summary of Bialek's proportional sharing algorithm [14]. Losses are first allocated to demands and then to generators [10].

In respect to demands, a total gross demand including losses  $P_D^G$  is defined as

$$P_D^G = P_D + L \quad \text{and} \quad P_D^G = \sum_{j=1}^{N_D} P_{Dj}^G \quad (19)$$

where  $P_{Dj}^G$  is the gross demand of bus  $j$ .

The total gross demand must equal the total generation so that  $P_G = P_D^G$ . Using the proportional sharing principle, the power balance in every bus of an equivalent lossless network becomes

$$P_i^G = P_{Gi} + \sum_{j \in \alpha_i} c_{ji} P_j^G \quad \text{where } i = 1, \dots, N \quad (20)$$

with

$$c_{ji} = \frac{P_{ji}^G}{P_j^G} \approx \frac{P_{ji}}{P_j} \quad (21)$$

$P_i^G$	gross power injected at bus $i$ ;
$P_{Gi}$	generation in bus $i$ ;
$\sum_{j \in \alpha_i} c_{ji} P_j^G$	power flow reaching bus $i$ from lines connected to it.
$\alpha_i$	set of buses from which power flows toward bus $i$ ;
$P_{ji}^G$	gross power flow from $j$ to $i$ ;
$P_{ji}$	actual power flow from $j$ to $i$ (measured in $j$ );
$P_j$	actual power injections in bus $j$ .

Equation (20) constitutes a system of linear equations that can be solved easily for  $P_i^G, i = 1, \dots, N$ . New generations and losses are then computed,



respectively, as

$$P_{Dj}^G = \frac{P_j^G}{P_j} P_{Dj} \text{ and } L_{Dj} = P_{Dj}^G - P_{Dj} \quad (22)$$

Losses are assigned to generators. Total gross generation including losses  $P_G^G$  is defined as

$$P_G^G = P_G + L \text{ and } P_G^G = \sum_{i=1}^{N_G} P_{Gi}^G \quad (23)$$

Where  $P_{Gi}^G$  is the gross generation of bus  $i$ , including losses.

The gross generation must be equal to the total demand, so that  $P_G^G = P_D$ . Using the proportional sharing principle, the power balance in bus  $i$  of an equivalent lossless network becomes

$$P_i^G = P_{Di} + \sum_{j \in \gamma i} c_{ji} P_j^G, \quad \text{where } i = 1, \dots, N \quad (24)$$

Where

$P_i^G$	gross power injected in bus $i$ ;
$P_{Di}$	demand in bus $i$ ;
$\sum_{j \in \gamma i} c_{ji} P_j^G$	power flow leaving bus $i$ ;
$\gamma i$	set of buses drawing power from bus $i$ ;

Equation (24) constitutes a system of linear equation that can be solved easily for  $P_i^G$ ,  $i = 1, \dots, N$ . New generations and losses are then computed respectively as

$$P_{Gi}^G = \frac{P_i^G}{P_i} P_{Gi} \quad \text{and} \quad L_{Gi} = P_{Gi} - P_{Gi}^G \quad (25)$$

In order to assign 50 % of losses to the generation and 50% to the demand, the final generation and demand per bus are computed as

$$P'_{Gi} = \frac{P_{Gi}^G + P_{Gi}}{2} \quad \text{and} \quad P'_{Dj} = \frac{P_{Dj}^G + P_{Dj}}{2} \quad (26)$$

Losses assigned to every generator and demand are, respectively,

$$L'_{Gi} = P_{Gi} - P'_{Gi} \quad \text{and} \quad L'_{Dj} = P'_{Dj} - P_{Dj}. \quad (27)$$

Generation and demand loss allocation factors are respectively computed as

$$K_{Gi} = 1 - \frac{P'_{Gi}}{P_{Gi}} \quad \text{and} \quad K_{Dj} = \frac{P'_{Dj}}{P_{Dj}} - 1 \quad (28)$$

### ***3.3.5 Predicting Power Loss in a Transaction***

Loss in a transaction is the difference between the generation's contribution to a demand at the generation end and the generation's contribution to a demand at the load bus. In order to implement a new direction involving competitive marketing of electric energy, it is necessary to know how the costs of providing electric energy vary. These variations the losses associated with generation, transportation and delivery of electricity. Learning coefficients enables learning of the relationship between a demand and the contributions to this demand through each possible transmission path based on the current and few past operational scenarios. Once these learning coefficients are obtained, they can be used to predict contribution of each generation to a retailer's future demand, and the share of the losses related to a transaction in a line. By predicting the losses associated with a transaction, it is possible to predict the power required at the delivery end of a line for meeting a certain portion of a retailer's future demand.

The learning coefficient can be kept updated, as and when new operational scenarios come up [15].

Loss in a transaction can be calculated using the following formula,

$$Loss_t = \frac{\alpha}{P_d} + \beta + \gamma P_d \quad (29)$$

where  $Loss_t$  = the loss in a transaction

$P_d$  = the total demand at the retailer's point in p.u.

$\alpha, \beta, \gamma$  = the learning coefficients

This equation represents a relationship between the transmission loss incurred while supplying a given load and the power demand.  $P_d$  is an independent variable while  $Loss_t$  is a dependent variable. If  $P_d$  and  $Loss_t$  are known for the past few scenarios, they can be used in equation (20) to obtain the coefficients  $\alpha, \beta, \gamma$ . These coefficients can then be used to predict loss associated to any given transaction. This method is proposed in [16].

For example, if the past three scenarios are known, then the following formula may be used

$$\begin{bmatrix} \alpha \\ \beta \\ \gamma \end{bmatrix} = \begin{bmatrix} \frac{1}{P_{d1}} & 1 & P_{d1} \\ \frac{1}{P_{d2}} & 1 & P_{d1} \\ \frac{1}{P_{d3}} & 1 & P_{d1} \end{bmatrix}^{-1} \begin{bmatrix} Loss_{t1} \\ Loss_{t2} \\ Loss_{t3} \end{bmatrix} \quad (30)$$

then the determined coefficients can be used in equation (20) to predict the power loss in a transaction for an oncoming operating scenario. The predicted losses are supposed to match the losses obtained from a power flow. Using

equation (22), we can then determine the percentage error to see if the predicted losses are valid. An error of 10% is acceptable [17].

$$\%Error = \left| \frac{Loss_{t4} - Loss_{t4pred}}{Loss_{t4}} \right| \times 100\% \quad (31)$$

### 3.4 The IEEE 24-Bus RTS System

For this project, the IEEE 24-bus RTS system [18] will be used to do power flows and tracing and determine transmission losses. Figure 5 shows the diagram of the system that will be used in the project.

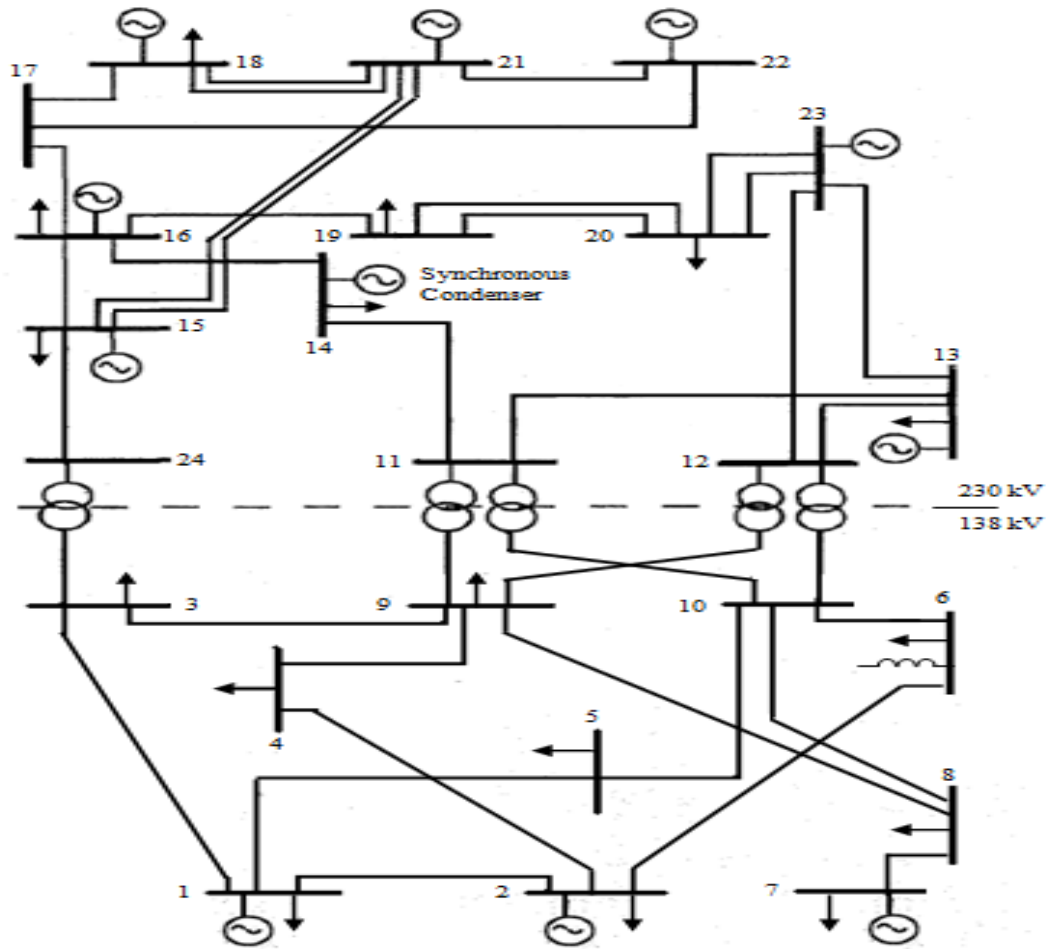


Figure 8: IEEE 24-bus RTS system

The bus load is assigned based on assumptions shown in table 1.

Table 1: IEEE 24-bus system bus data

Bus number	Bus load	Load		If peak is 10% higher	
	% system load	MW	MVar	MW	MVar
101	3.8	108	22	118.8	24.2
102	3.4	97	20	106.7	22
103	6.3	180	37	198	40.7
104	2.6	74	15	81.4	16.5
105	2.5	71	14	78.1	15.4
106	4.8	136	28	149.5	30.8
107	4.4	125	25	137.5	27.5
108	6	171	35	188.1	38.5
109	6.1	175	36	192.5	39.6
110	6.8	195	40	214.5	44
111	0	0	0	0	0
112	0	0	0	0	0
113	9.3	265	54	219.5	59.4
114	6.8	195	39	213.4	42.9
115	11.1	317	64	348.7	70.4
116	3.5	100	20	110	22
117	0	0	0	0	0
118	11.7	333	68	366.3	74.8
119	6.4	181	37	199.1	40.7
120	4.5	128	26	140.8	28.6
121	0	0	0	0	0
122	0	0	0	0	0
123	0	0	0	0	0
124	0	0	0	0	0

## **CHAPTER 4**

### **RESULTS AND DISCUSSIONS**

#### **4.1 Power Flow Simulation**

Appendix A and appendix B show power flow programs in m-file. These programs are used to run the power flow tracing of the system in figure 5. The bus data and generation data is specified in the m-file in appendix A, and the code used to do the power flow is specified in appendix B. Appendix C shows the results of the power flow, the load flow among the buses and the losses encountered. Matpower was used to run the simulation. The losses from the simulation are tabulated in table 2; the results simply show power losses between the buses after power tracing is done.

#### **4.2 Solving Loss Allocation Algorithms**

Appendix D shows the matlab code used to solve the loss allocation methods. The methods presented here are pro rata, ITL, proportional sharing and U-ITL algorithms. The results of the power flow from the 24 bus RTS are used to solve these algorithms. Table 6 shows the results of the 24 bus RTS power flow obtained by using matpower.

The loss allocation is performed for both the generation and demands. In section 3.3 of this report, the formulas of the loss allocation methods have been presented. These methods are used together with the system data in table 1 and the power flow results in table 2 to calculate the transmission losses. Table 3 and

table 4 show the resulting losses obtained for the different methods.

Table 2: Power flow results

Branch #	Bus		From Bus Injection		To Bus Injection		Loss( $I^2 \cdot Z$ )	
	From	To	P(MW)	Q(MVAr)	P(MW)	Q(MVAr)	P(MW)	Q(MVAr)
1	1	2	10.60	-26.67	-10.6	-22.70	0.003	0.02
2	1	3	-5.21	20.40	5.50	-25.12	0.29	1.14
3	1	5	58.60	5.17	-57.60	-4.48	0.71	2.74
4	2	4	38.01	19.14	-37.43	-20.46	0.58	2.23
5	2	6	47.60	-0.85	-46.54	-0.53	1.05	5.07
6	3	9	17.15	-15.26	-17.00	12.65	0.15	0.58
7	3	24	-202.65	3.39	203.68	33.91	1.02	37.3
8	4	9	-36.57	5.46	36.94	-6.82	0.37	1.44
9	5	10	-13.10	-9.16	13.15	6.85	0.05	0.2
10	6	10	-89.46	-129.95	90.54	-121.34	1.09	4.73
11	7	8	115.00	26.79	-112.88	-20.31	2.12	8.18
12	8	9	-36.57	3.12	37.17	-5.28	0.59	2.29
14	9	11	-106.49	-12.56	106.77	22.76	0.28	10.2
15	9	12	-125.62	-24.00	126.02	38.51	0.40	14.51
16	10	11	-150.16	35.61	150.70	-25.95	0.54	19.66
19	11	14	-161.26	46.26	162.83	-42.61	1.57	12.18
20	12	13	-62.32	-34.35	62.61	26.39	0.29	2.25
21	12	23	-234.75	-4.18	241.57	35.57	6.812	53.07
22	13	23	-232.54	7.46	238.34	18.26	5.80	45.2
25	15	21	-351.36	-6.04	358.92	53.90	7.56	58.83
26	15	24	206.63	45.96	-203.68	-33.91	2.96	22.89
27	16	17	-396.34	-14.11	401.36	47.73	5.02	39.37
28	16	19	130.53	-6.73	-130.04	5.53	0.49	3.81
30	17	22	-160.09	9.31	163.35	-7.90	3.27	25.5
31	18	21	-175.30	23.08	176.24	-21.71	0.94	7.38
32	19	20	-50.96	-42.53	51.16	35.37	0.20	1.56
33	20	23	-179.16	-61.37	180.10	63.65	0.94	7.21
34	21	22	-135.16	15.37	136.65	-19.51	1.48	11.57
						Total	51.246	454.77

Table 3 shows the losses allocated to the generators, and table 4 shows the losses allocated to the loads.

Table 3: Transmission losses allocated to generators

Bus no	Real power loss(MW)			
	PR	PS	ITL	U-ITL
1	1.5192	1.080	9.6556	16.8186
2	1.5192	1.6800	8.2394	15.4705
7	2.1198	2.1200	7.4980	17.7557
13	1.6539	5.4400	-8.6527	0.0000
15	1.899	9.3300	-7.5730	2.2606
16	1.369	3.7800	10.1251	16.5193
18	3.533	0.2200	21.4494	38.1571
21	3.533	2.0000	3.5928	21.1050
22	2.6497	0	3.5928	16.6890
23	5.8294	0	3.5928	32.5521



Table 4: Losses allocated to loads

Bus no	Real power losses(MW)			
	PR	PS	ITL	U-ITL
1	0.9711	0.5400	7.6667	1.3656
2	0.8721	0.8400	5.8759	2.3261
3	1.6184	0.6750	-4.5432	21.1511
4	0.6654	0.1850	-4.5432	11.6154
5	0.6384	0.0250	-4.5432	11.3458
6	1.2228	0.5350	-4.5432	17.1964
7	1.1239	1.0600	4.9383	5.8726
8	1.5375	0.4600	-4.5432	20.3545
9	1.5735	1.4050	-4.5432	20.7162
10	1.7533	0.5900	-4.5432	22.5098
13	2.3917	2.7200	-15.4850	40.7292
14	1.7443	3.5250	-4.5432	22.4155
15	2.8502	4.6650	-14.1197	43.9184
16	0.8991	1.8900	8.2604	0.0000
18	2.9941	0.1100	22.5806	5.3721
19	1.6274	0.1200	-4.5432	21.2489
20	1.1509	0.2900	-4.5432	16.4779
Total	46.23	45.29	25.8057	413.77

From table 4, we can notice that for pro rata (PR) and proportional sharing (PS), the losses are always positive, however, for incremental loss (ITL), there are negative losses. That is because for pro rata and proportional sharing, the losses allocated to the generators and loads are supposed to be positive all the

time. And for ITL, the losses allocated can be negative. These negative losses can be interpreted as cross subsidies. The unsubsidized ITL (U-ITL) method eliminates the negative losses if they are undesirable.

The losses allocated to generators and demands in table 3 and table 4 is plotted to show and shown in figure 9 and figure 10 below.

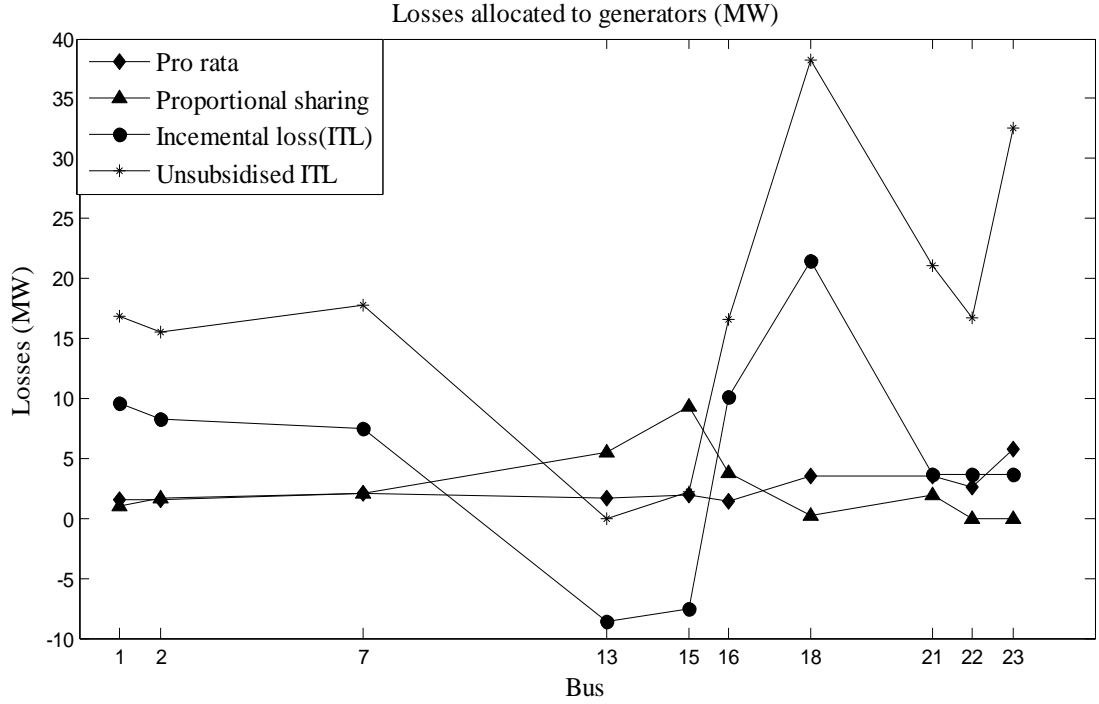


Figure 9: Losses allocated to generators

In figure 9 above, there are plots of the losses allocated to generators. From just observing, we can see that the losses obtained by using incremental loss method differs significantly from the ones obtained using pro rata and proportional sharing. This may be a result of the different ways in which the methods address the topological considerations of the network. The same applies for the plots of the losses allocated to loads in figure 10.

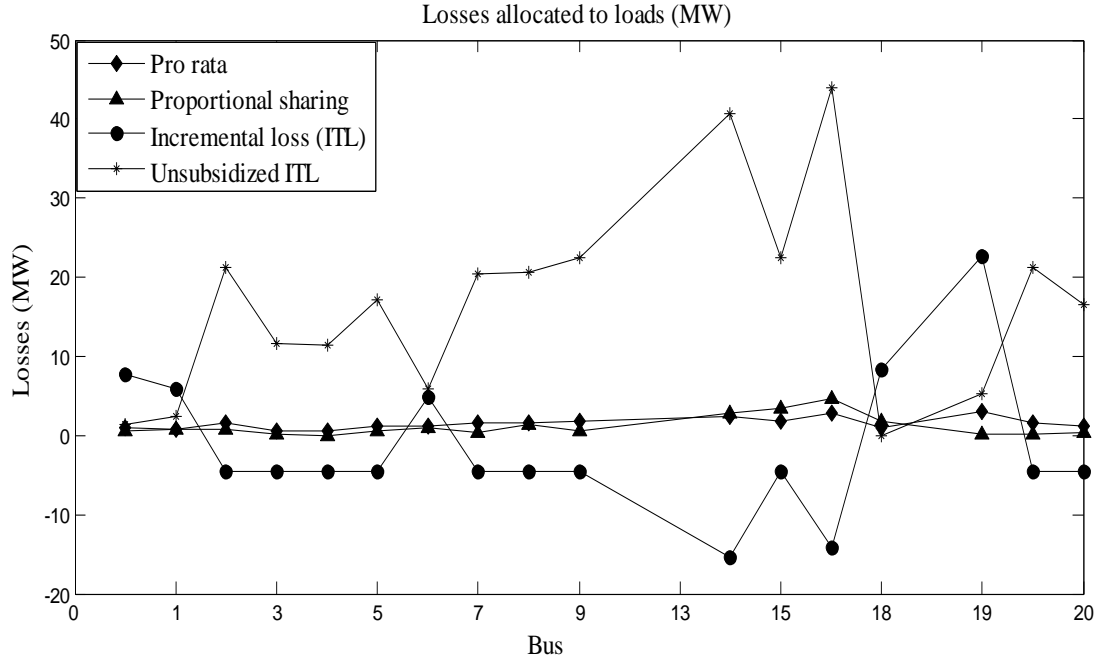


Figure 10: Losses allocated to loads

The four different methods were used to allocate the losses to each load and generator as the results are shown in figure 9 and 10. The ITL method produces some negative losses, even though other methods produce positive losses. This happens because ITL is highly dependent on choosing a slack generator bus.

The results for pro rata and proportional sharing methods are always different. This is because the pro rata method neglects the network and only depends on the level of power produced by generators or power consumed by loads. However, as seen in figure 9 and 10, the pattern for these two methods is almost similar. The main disadvantage of the pro rata method is that it is unfair to some participants even though they have good positioning in the market. For example, loads do not get financial incentives even though they are close to generators. This method is also unable to trace power flows.

The ITL and PS methods also produce completely different results. This is because the ITL coefficients are chosen from changes of power injection

at the selected bus while the slack generator bus either increases or decreases power automatically. The total allocation of the ITL is much different from the total real losses. To minimize this difference some normalization has to be performed on the method. This method fails to separate contributions of power between the selected bus and the slack bus generator.

The PS method is able to trace the contribution of losses caused by each generator and load. This method never allocates negative losses because it follows the direction of the power flow. The method uses an assumption to separate power flows from different sources, but the sum of the total allocation is consistent with the real total losses. As a result this method is more reasonable than other methods and can be easily understood by each participant.

The qualitative and quantitative measurements are used to determine which method is better. Table 5 shows the measurements.

Table 5: Qualitative and quantitative measurements

Characteristics	Methods			
	Prorata	PS	ITL	U_ITL
Consistent with a solved load flow	No	Yes	Yes	Yes
Only giving positive allocation	Yes	Yes	No	Yes
Not volatile	Yes	Yes	No	No
Able to trace the power in and out	No	Yes	No	No
The total sum of the allocations must be consistent to the real total losses	Yes	Yes	No	No

According to table 6, the PS method is the best of the four methods. This is because it can allocate the losses that have the total sum as the real losses and is therefore consistent with a solved power flow solution. Although this method

uses assumption, this assumption has been proved in [19].

The pro rata method may be applied in a network where the loads and generators are close to one another, as it neglects the position of loads and generators in the network. This method is easy to understand and implement. Its pattern is similar to that of the PS method. It is by far the most popular method around the world.

The ITL method is not recommended because the allocation produces negative losses and the results are volatile depending on the choice of a slack generator bus. This method also needs a normalization procedure to match the total sum of the loss allocations to the real total losses.

The U-ITL method gets rid of the negative losses produces by the ITL method. But the method still needs normalization to match the total sum of the loss allocation to the real total losses.

#### **4.3 Predicting Power Loss in a Transaction**

Loss prediction was performed and tables 6-8 present the results. The past four scenarios were used to predict the fifth scenarios. These scenarios were created by continuously increasing the original demand by 10% and calculating the losses for each scenario. All this information was then combined and used to predict the losses for the fifth scenario.

Table 6 shows the original load, and how it is continuously increased by 10 %.  $P_d$  = load power;  $P_{d1}$  =  $P_d$  increased by 10 %;  $P_{d2}$  =  $P_{d1}$  increased by 10 %;  $P_{d3}$  =  $P_{d2}$  increased by 10 %;  $P_{d4}$  =  $P_{d3}$  increased by 10 %.

Table 6: Load power with 10 % increments

Bus no	Pd (pu)	Pd1 (pu)	Pd2 (pu)	Pd3 (pu)	Pd4 (pu)
1	1.08	1.188	1.3068	1.4375	1.5812
2	0.97	1.067	1.1137	1.2911	1.4202
3	1.80	1.980	2.1780	2.3958	2.6354
4	0.74	0.814	0.8954	0.9849	1.0834
5	0.71	0.781	0.8591	0.9450	1.0395
6	1.36	1.496	1.6456	1.8102	1.9912
7	1.25	1.375	1.5125	1.6638	1.8301
8	1.71	1.881	2.0691	2.2760	2.5036
9	1.75	1.925	2.1175	2.3293	2.5622
10	1.95	2.145	2.3595	2.5955	2.8550
13	2.65	2.915	3.2065	3.5272	3.8799
14	1.94	2.134	2.3474	2.5822	2.8404
15	3.17	3.487	3.8357	4.2193	4.6412
16	1.00	1.100	1.2100	1.3310	1.4641
18	3.33	3.663	4.0293	4.4322	4.8754
19	1.81	1.991	2.1901	2.4091	2.6500
20	1.28	1.408	1.5488	1.7037	1.8740

Load flow is performed for all the scenarios in table 6 using matlab, and the corresponding losses are tabulated in table 7.

For table 7 below, LossT corresponds to Pd; LossT1 corresponds to Pd1; LossT2 corresponds to Pd2; LossT3 corresponds to Pd3; LossT4 corresponds to Pd4.

Table 7: Losses obtained by load flow corresponding to 10% increment

Bus no	LossT	LossT1	LossT2	LossT3	LossT4
1	0.01870	0.00989	0.00999	0.01224	0.01920
2	0.01680	0.01417	0.01270	0.01364	0.01994
3	0.01353	0.01205	0.01257	0.01593	0.02347
4	0.00364	0.00720	0.01229	0.02045	0.03350
5	0.00046	0.00164	0.00448	0.00950	0.02000
6	0.01670	0.01568	0.02261	0.03228	0.04629
7	0.02118	0.01798	0.01584	0.01589	0.02081
8	0.00907	0.01827	0.03391	0.05931	0.10109
9	0.00646	0.01046	0.01629	0.02475	0.03736
10	0.01187	0.01773	0.02588	0.03740	0.05430
13	0.05438	0.02826	0.00933	0.00133	0.01049
14	0.07054	0.06000	0.04952	0.03936	0.02984
15	0.09335	0.09096	0.08968	0.09024	0.09415
16	0.03786	0.03031	0.02392	0.01938	0.01786
18	0.00222	0.00254	0.00292	0.00336	0.00384
19	0.00226	0.00506	0.01066	0.02014	0.03538
20	0.00582	0.01038	0.01740	0.02776	0.04294

Now that we have relevant information for the past scenarios, the demands and their losses, we use then to calculate the learning coefficients. These coefficients can then be used predict any of the oncoming scenario.

With the information that has been acquired in table 6 table 7, the coefficients  $\alpha$ ,  $\beta$  and  $\gamma$  can now be calculated using equation (29).Table 8 shows the results of the calculation.

Table 8: Learning coefficients

Bus no	A	$\beta$	$\gamma$
1	0.1465	-0.2265	0.0952
2	0.1572	-0.2524	0.1118
3	0.3181	-0.2998	0.0764
4	0.1201	-0.3254	0.2273
5	0.0853	-0.2353	0.1635
6	0.1764	-0.2788	0.1180
7	0.1905	-0.2251	0.0760
8	0.8883	-1.0397	0.3114
9	0.2270	-0.2730	0.0860
10	0.3158	-0.3448	0.1004
13	2.1537	-1.930	0.1655
14	0.1682	0.0143	-0.0155
15	0.3954	-0.1127	0.0259
16	0.1578	-0.1796	0.0604
18	0.0046	-0.0037	0.0014
19	0.3809	-0.4161	0.1155
20	0.2140	-0.3500	0.1480

Since now we have  $\alpha$ ,  $\beta$  and  $\gamma$ , we can predict the losses if the load in table 6 is increased by another 10 %, i.e. losses when the load power is Pd4. Equation (30) is used for the prediction and the results are tabulated in table 9. Percentage error can be calculated to see how accurate the predication is. Equation (31) is used to calculate the error. The acceptable error is within 10%.



Table 9: Losst4pred for Pd4 compared with Losst4 from load flow

Bus no	LossT4(pu)	LossT4pred(pu)	Percentage Error (%)
1	0.01920	0.0167	13.02
2	0.01994	0.0170	14.7
3	0.02347	0.0222	5.4
4	0.03350	0.0318	5.1
5	0.02000	0.0167	16.5
6	0.04629	0.0448	3.2
7	0.02081	0.0181	13.02
8	0.10109	0.0947	6.3
9	0.03736	0.0359	3.91
10	0.05430	0.0524	3.40
13	0.01049	0.0042	59.96
14	0.02984	0.0294	1.47
15	0.09415	0.0926	1.65
16	0.01786	0.0166	7.05
18	0.00384	0.0039	1.56
19	0.03538	0.0336	5.03
20	0.04294	0.0416	3.12

As the results can be seen, the losses have been predicted successfully, as most of the values fall within the acceptable 10% error. Even the values that fall outside the 10% don't are still close to the range. Only one prediction is done totally unsuccessfully, so we can safely conclude that this method is suitable to be used for loss prediction.

## **CHAPTER 5**

### **CONCLUSIONS AND RECOMMENDATIONS**

#### **5.1 Conclusions**

A 24 bus RTS was used for simulation to obtain the power flow. The results of the power flow were then used together with the loss allocation algorithms in section 3.3 of the report to allocate the losses to generators and loads using pro rata, proportional sharing and incremental loss methods. These results were tabulated and plotted and the results were explained in chapter 4.

By far the pro rata is the most popular method, even though it neglects networks and it is not able to trace power flows. It is unfair to certain market participants.

The ITL method produces volatile results and negative losses. It also needs to be normalized in order to give the total sum of allocations that is consistent with the real total losses.

The U-ITL gets rid of the negative losses produced by the ITL method, but still needs to be normalized in order to give the total sum of allocations that is the same as the real total losses.

The PS method is the most reasonable of the four methods. It is able to trace the flow of power in and out at each bus, from generators and loads vice versa. This method is also able to trace the contributions of losses caused by each

load or generator. The results of this method are always positive and the total sum of loss allocations is consistent with the total sum of the real losses.

Lastly loss prediction was performed was done and the results were satisfactory. The adopted method for prediction proved to be reliable as the predicted values were close enough to those acquired using load flow.

## **5.2 Recommendations**

To take the research a little further, the study can be focus on the weekly power consumption of a certain area (for example place of residence). Allocation and prediction can then be done on the weekly power generation, demand and losses. The actual power can then be obtained and compared with the predicted power to see if the prediction was successful.

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## APPENDICES

# APPENDIX A

## M-FILE SPECIFYING SYTEM DATA

```
function mpc = case24_ieee_rts
mpc.version = '2';

%%----- Power Flow Data -----%%
%% system MVA base
mpc.baseMVA = 100;

%% bus data
% bus_i type Pd Qd Gs Bs area Vm Va baseKV zone Vmax
Vmin
mpc.bus = [
    1 2 108 22 0 0 1 1 0 138 1 1.05 0.95;
    2 2 97 20 0 0 1 1 0 138 1 1.05 0.95;
    3 1 180 37 0 0 1 1 0 138 1 1.05 0.95;
    4 1 74 15 0 0 1 1 0 138 1 1.05 0.95;
    5 1 71 14 0 0 1 1 0 138 1 1.05 0.95;
    6 1 136 28 0 -100 2 1 0 138 1 1.05 0.95;
    7 2 125 25 0 0 2 1 0 138 1 1.05 0.95;
    8 1 171 35 0 0 2 1 0 138 1 1.05 0.95;
    9 1 175 36 0 0 1 1 0 138 1 1.05 0.95;
    10 1 195 40 0 0 2 1 0 138 1 1.05 0.95;
    11 1 0 0 0 0 3 1 0 230 1 1.05 0.95;
    12 1 0 0 0 0 3 1 0 230 1 1.05 0.95;
    13 3 265 54 0 0 3 1 0 230 1 1.05 0.95;
    14 2 194 39 0 0 3 1 0 230 1 1.05 0.95;
    15 2 317 64 0 0 4 1 0 230 1 1.05 0.95;
    16 2 100 20 0 0 4 1 0 230 1 1.05 0.95;
    17 1 0 0 0 0 4 1 0 230 1 1.05 0.95;
    18 2 333 68 0 0 4 1 0 230 1 1.05 0.95;
    19 1 181 37 0 0 3 1 0 230 1 1.05 0.95;
    20 1 128 26 0 0 3 1 0 230 1 1.05 0.95;
    21 2 0 0 0 0 4 1 0 230 1 1.05 0.95;
    22 2 0 0 0 0 4 1 0 230 1 1.05 0.95;
    23 2 0 0 0 0 3 1 0 230 1 1.05 0.95;
    24 1 0 0 0 0 4 1 0 230 1 1.05 0.95;
];

%% generator data
% bus Pg Qg Qmax Qmin Vg mBase status Pmax Pmin Pc1
Pc2 Qc1min Qc1max Qc2min Qc2max ramp_agc ramp_10 ramp_30 ramp_q
apf % Unit Code
mpc.gen = [
    1 10 0 10 0 1.035 100 1 20 16 0 0 0 0 0 0
    0 0 0 0 0; % U20
    1 10 0 10 0 1.035 100 1 20 16 0 0 0 0 0 0
    0 0 0 0 0; % U20
    1 76 0 30 -25 1.035 100 1 76 15.2 0 0 0 0 0
    0 0 0 0 0 0; % U76
    1 76 0 30 -25 1.035 100 1 76 15.2 0 0 0 0 0
    0 0 0 0 0 0; % U76
    2 10 0 10 0 1.035 100 1 20 16 0 0 0 0 0
    0 0 0 0 0; % U20
    2 10 0 10 0 1.035 100 1 20 16 0 0 0 0 0
    0 0 0 0 0; % U20
    2 76 0 30 -25 1.035 100 1 76 15.2 0 0 0 0 0
    0 0 0 0 0 0; % U76
];
```



```

0 2 76 0 30 -25 1.035 100 1 76 15.2 0 0 0 0 0
0 0 0 0 0 0; % U76
0 7 80 0 60 0 1.025 100 1 100 25 0 0 0 0 0
0 0 0 0 0; % U100
0 7 80 0 60 0 1.025 100 1 100 25 0 0 0 0 0
0 0 0 0 0; % U100
0 7 80 0 60 0 1.025 100 1 100 25 0 0 0 0 0
0 0 0 0 0; % U100
0 13 95.1 0 80 0 1.02 100 1 197 69 0 0 0 0 0
0 0 0 0 0 0; % U197
0 13 95.1 0 80 0 1.02 100 1 197 69 0 0 0 0 0
0 0 0 0 0 0; % U197
0 13 95.1 0 80 0 1.02 100 1 197 69 0 0 0 0 0
0 0 0 0 0 0; % U197
0 14 0 35.3 200 -50 0.98 100 1 0 0 0 0 0 0
0 0 0 0 0 0; % SynCond
0 15 12 0 6 0 1.014 100 1 12 2.4 0 0 0 0 0
0 0 0 0 0; % U12
0 15 12 0 6 0 1.014 100 1 12 2.4 0 0 0 0 0
0 0 0 0 0; % U12
0 15 12 0 6 0 1.014 100 1 12 2.4 0 0 0 0 0
0 0 0 0 0; % U12
0 15 12 0 6 0 1.014 100 1 12 2.4 0 0 0 0 0
0 0 0 0 0; % U12
0 15 155 0 80 -50 1.014 100 1 155 54.3 0 0 0 0 0
0 0 0 0 0 0; % U155
0 16 155 0 80 -50 1.017 100 1 155 54.3 0 0 0 0 0
0 0 0 0 0 0; % U155
0 18 400 0 200 -50 1.05 100 1 400 100 0 0 0 0 0
0 0 0 0 0; % U400
0 21 400 0 200 -50 1.05 100 1 400 100 0 0 0 0 0
0 0 0 0 0; % U400
0 22 50 0 16 -10 1.05 100 1 50 10 0 0 0 0 0
0 0 0 0 0; % U50
0 22 50 0 16 -10 1.05 100 1 50 10 0 0 0 0 0
0 0 0 0 0; % U50
0 22 50 0 16 -10 1.05 100 1 50 10 0 0 0 0 0
0 0 0 0 0; % U50
0 22 50 0 16 -10 1.05 100 1 50 10 0 0 0 0 0
0 0 0 0 0; % U50
0 22 50 0 16 -10 1.05 100 1 50 10 0 0 0 0 0
0 0 0 0 0; % U50
0 23 155 0 80 -50 1.05 100 1 155 54.3 0 0 0 0 0
0 0 0 0 0 0; % U155
0 23 155 0 80 -50 1.05 100 1 155 54.3 0 0 0 0 0
0 0 0 0 0 0; % U155
0 23 350 0 150 -25 1.05 100 1 350 140 0 0 0 0 0
0 0 0 0 0; % U350
];

```

```

%% branch data
% fbus tbus r x b rateA rateB rateC ratio angle
status angmin angmax
mpc.branch = [
1 2 0.0026 0.0139 0.4611 175 250 200 0 0 1 -360 360;
1 3 0.0546 0.2112 0.0572 175 208 220 0 0 1 -360 360;
1 5 0.0218 0.0845 0.0229 175 208 220 0 0 1 -360 360;
2 4 0.0328 0.1267 0.0343 175 208 220 0 0 1 -360 360;
2 6 0.0497 0.192 0.052 175 208 220 0 0 1 -360 360;
3 9 0.0308 0.119 0.0322 175 208 220 0 0 1 -360 360;

```

```

3 24 0.0023 0.0839 0 400 510 600 1.03 0 1 -360 360;
4 9 0.0268 0.1037 0.0281 175 208 220 0 0 1 -360 360;
5 10 0.0228 0.0883 0.0239 175 208 220 0 0 1 -360 360;
6 10 0.0139 0.0605 2.459 175 193 200 0 0 1 -360 360;
7 8 0.0159 0.0614 0.0166 175 208 220 0 0 1 -360 360;
8 9 0.0427 0.1651 0.0447 175 208 220 0 0 1 -360 360;
8 10 0.0427 0.1651 0.0447 175 208 220 0 0 1 -360 360;
9 11 0.0023 0.0839 0 400 510 600 1.03 0 1 -360 360;
9 12 0.0023 0.0839 0 400 510 600 1.03 0 1 -360 360;
10 11 0.0023 0.0839 0 400 510 600 1.02 0 1 -360 360;
10 12 0.0023 0.0839 0 400 510 600 1.02 0 1 -360 360;
11 13 0.0061 0.0476 0.0999 500 600 625 0 0 1 -360 360;
11 14 0.0054 0.0418 0.0879 500 625 625 0 0 1 -360 360;
12 13 0.0061 0.0476 0.0999 500 625 625 0 0 1 -360 360;
12 23 0.0124 0.0966 0.203 500 625 625 0 0 1 -360 360;
13 23 0.0111 0.0865 0.1818 500 625 625 0 0 1 -360 360;
14 16 0.005 0.0389 0.0818 500 625 625 0 0 1 -360 360;
15 16 0.0022 0.0173 0.0364 500 600 625 0 0 1 -360 360;
15 21 0.0063 0.049 0.103 500 600 625 0 0 1 -360 360;
15 21 0.0063 0.049 0.103 500 600 625 0 0 1 -360 360;
15 24 0.0067 0.0519 0.1091 500 600 625 0 0 1 -360 360;
16 17 0.0033 0.0259 0.0545 500 600 625 0 0 1 -360 360;
16 19 0.003 0.0231 0.0485 500 600 625 0 0 1 -360 360;
17 18 0.0018 0.0144 0.0303 500 600 625 0 0 1 -360 360;
17 22 0.0135 0.1053 0.2212 500 600 625 0 0 1 -360 360;
18 21 0.0033 0.0259 0.0545 500 600 625 0 0 1 -360 360;
18 21 0.0033 0.0259 0.0545 500 600 625 0 0 1 -360 360;
19 20 0.0051 0.0396 0.0833 500 600 625 0 0 1 -360 360;
19 20 0.0051 0.0396 0.0833 500 600 625 0 0 1 -360 360;
20 23 0.0028 0.0216 0.0455 500 600 625 0 0 1 -360 360;
20 23 0.0028 0.0216 0.0455 500 600 625 0 0 1 -360 360;
21 22 0.0087 0.0678 0.1424 500 600 625 0 0 1 -360 360;
];

%%----- OPF Data -----%%
%% area data
% area refbus
mpc.areas = [
1 1;
2 3;
3 8;
4 6;
];

%% generator cost data
% 1 startup shutdown n x1 y1 ... xn yn
% 2 startup shutdown n c(n-1) ... c0
mpc.gencost = [
Qmax Unit Code
2 1500 0 3 0 130 400.6849; % 1 16 20 0 10 U20
2 1500 0 3 0 130 400.6849; % 1 16 20 0 10 U20
2 1500 0 3 0.014142 16.0811 212.3076; % 1 15.2
76 -25 30 U76
2 1500 0 3 0.014142 16.0811 212.3076; % 1 15.2
76 -25 30 U76
2 1500 0 3 0 130 400.6849; % 2 16 20 0 10 U20
2 1500 0 3 0 130 400.6849; % 2 16 20 0 10 U20
2 1500 0 3 0.014142 16.0811 212.3076; % 2 15.2
76 -25 30 U76
2 1500 0 3 0.014142 16.0811 212.3076; % 2 15.2
76 -25 30 U76
2 1500 0 3 0.052672 43.6615 781.521; % 7 25 100
0 60 U100
];

```

	2	1500	0	3	0.052672	43.6615	781.521;	%	7	25	100	
0	60	U100										
	2	1500	0	3	0.052672	43.6615	781.521;	%	7	25	100	
0	60	U100										
	2	1500	0	3	0.00717	48.5804	832.7575;	%	13	69	197	0
80	U197											
	2	1500	0	3	0.00717	48.5804	832.7575;	%	13	69	197	0
80	U197											
	2	1500	0	3	0.00717	48.5804	832.7575;	%	13	69	197	0
80	U197											
	2	1500	0	3	0	0	0;	%	14			
												SynCond
	2	1500	0	3	0.328412	56.564	86.3852;	%	15	2.4	12	
0	6	U12										
	2	1500	0	3	0.328412	56.564	86.3852;	%	15	2.4	12	
0	6	U12										
	2	1500	0	3	0.328412	56.564	86.3852;	%	15	2.4	12	
0	6	U12										
	2	1500	0	3	0.328412	56.564	86.3852;	%	15	2.4	12	
0	6	U12										
	2	1500	0	3	0.328412	56.564	86.3852;	%	15	2.4	12	
0	6	U12										
	2	1500	0	3	0.008342	12.3883	382.2391;	%	15	54.3		
155	-50	80	U155									
	2	1500	0	3	0.008342	12.3883	382.2391;	%	16	54.3		
155	-50	80	U155									
	2	1500	0	3	0.000213	4.4231	395.3749;	%	18	100	400	
-50	200	U400										
	2	1500	0	3	0.000213	4.4231	395.3749;	%	21	100	400	
-50	200	U400										
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0	0.001	0.001;	%	22	10	50	-10 16 U50
	2	1500	0	3	0.008342	12.3883	382.2391;	%	23	54.3		
155	-50	80	U155									
	2	1500	0	3	0.008342	12.3883	382.2391;	%	23	54.3		
155	-50	80	U155									
	2	1500	0	3	0.004895	11.8495	665.1094;	%	23	140	350	
-25	150	U350										
1;												

## APPENDIX B

### POWER FLOW PRORAM

```

function [MVAbase, bus, gen, branch, success, et] = ...
    runpf(casedata, mpopt, fname, solvedcase)
[PQ, PV, REF, NONE, BUS_I, BUS_TYPE, PD, QD, GS, BS, BUS_AREA, VM, ...
    VA, BASE_KV, ZONE, VMAX, VMIN, LAM_P, LAM_Q, MU_VMAX, MU_VMIN] =
idx_bus;
[F_BUS, T_BUS, BR_R, BR_X, BR_B, RATE_A, RATE_B, RATE_C, ...
    TAP, SHIFT, BR_STATUS, PF, QF, PT, QT, MU_SF, MU_ST, ...
    ANGMIN, ANGMAX, MU_ANGMIN, MU_ANGMAX] = idx_brch;
[GEN_BUS, PG, QG, QMAX, QMIN, VG, MBASE, GEN_STATUS, PMAX, PMIN, ...
    MU_PMAX, MU_PMIN, MU_QMAX, MU_QMIN, PC1, PC2, QC1MIN, QC1MAX, ...
    QC2MIN, QC2MAX, RAMP_AGC, RAMP_10, RAMP_30, RAMP_Q, APF] = idx_gen;

%% default arguments
if nargin < 4
    solvedcase = ''; % don't save solved case
    if nargin < 3
        fname = ''; % don't print results to a file
        if nargin < 2
            mpopt = mpoption; % use default options
            if nargin < 1
                casedata = 'case9'; % default data file is 'case9.m'
            end
        end
    end
end

%% options
verbose = mpopt(31);
qlim = mpopt(6); % enforce Q limits on gens?
dc = mpopt(10); % use DC formulation?

%% read data
mpc = loadcase(casedata);

%% add zero columns to branch for flows if needed
if size(mpc.branch,2) < QT
    mpc.branch = [ mpc.branch zeros(size(mpc.branch, 1), QT-
size(mpc.branch,2)) ];
end

%% convert to internal indexing
mpc = ext2int(mpc);
[baseMVA, bus, gen, branch] = deal(mpc.baseMVA, mpc.bus, mpc.gen,
mpc.branch);

%% get bus index lists of each type of bus
[ref, pv, pq] = bustypes(bus, gen);

%% generator info
on = find(gen(:, GEN_STATUS) > 0); % which generators are on?
gbus = gen(on, GEN_BUS); % what buses are they at?

%%----- run the power flow -----
t0 = clock;
if verbose > 0
    v = mpver('all');
    fprintf('\nMATPOWER Version %s, %s', v.Version, v.Date);
end

```

```

if dc % DC formulation
    if verbose > 0
        fprintf(' -- DC Power Flow\n');
    end
    %% initial state
    Va0 = bus(:, VA) * (pi/180);

    %% build B matrices and phase shift injections
    [B, Bf, Pbusinj, Pfinj] = makeBdc(baseMVA, bus, branch);

    %% compute complex bus power injections (generation - load)
    %% adjusted for phase shifters and real shunts
    Pbus = real(makeSbus(baseMVA, bus, gen)) - Pbusinj - bus(:, GS) /
baseMVA;

    %% "run" the power flow
    Va = dcpf(B, Pbus, Va0, ref, pv, pq);

    %% update data matrices with solution
    branch(:, [QF, QT]) = zeros(size(branch, 1), 2);
    branch(:, PF) = (Bf * Va + Pfinj) * baseMVA;
    branch(:, PT) = -branch(:, PF);
    bus(:, VM) = ones(size(bus, 1), 1);
    bus(:, VA) = Va * (180/pi);
    %% update Pg for swing generator (note: other gens at ref bus are
accounted for in Pbus)
    %% Pg = Pinj + Pload + Gs
    %% newPg = oldPg + newPinj - oldPinj
    refgen = find(gbus == ref); % which is(are) the
reference gen(s)?
    gen(on(refgen(1)), PG) = gen(on(refgen(1)), PG) + (B(ref, :) * Va -
Pbus(ref)) * baseMVA;

    success = 1;
else % AC formulation
    if verbose > 0
        fprintf(' -- AC Power Flow '); % solver name and \n added
later
    end
    %% initial state
    % V0 = ones(size(bus, 1), 1); % flat start
    V0 = bus(:, VM) .* exp(sqrt(-1) * pi/180 * bus(:, VA));
    V0(gbus) = gen(on, VG) ./ abs(V0(gbus)) .* V0(gbus);

    if qlim
        ref0 = ref; % save index and angle of
        Varef0 = bus(ref0, VA); % original reference bus
        limited = []; % list of indices of gens @
Q limits
        fixedQg = zeros(size(gen, 1), 1); % Qg of gens at Q limits
    end
    repeat = 1;
    while (repeat)
        %% build admittance matrices
        [Ybus, Yf, Yt] = makeYbus(baseMVA, bus, branch);

        %% compute complex bus power injections (generation - load)
        Sbus = makeSbus(baseMVA, bus, gen);

        %% run the power flow
        alg = mpopt(1);
        if alg == 1
            [V, success, iterations] = newtonpf(Ybus, Sbus, V0, ref, pv,
pq, mpopt);
        end
    end
end

```

```

elseif alg == 2 || alg == 3
    [Bp, Bpp] = makeB(baseMVA, bus, branch, alg);
    [V, success, iterations] = fdpf(Ybus, Sbus, V0, Bp, Bpp,
ref, pv, pq, mpopt);
elseif alg == 4
    [V, success, iterations] = gausspf(Ybus, Sbus, V0, ref, pv,
pq, mpopt);
else
    error('Only Newton's method, fast-decoupled, and Gauss-
Seidel power flow algorithms currently implemented.');
```

end

```

    %% update data matrices with solution
    [bus, gen, branch] = pfsoln(baseMVA, bus, gen, branch, Ybus, Yf,
Yt, V, ref, pv, pq);

    if qlim                %% enforce generator Q limits
        %% find gens with violated Q constraints
        mx = find( gen(:, GEN_STATUS) > 0 & gen(:, QG) > gen(:,
QMAX) );
        mn = find( gen(:, GEN_STATUS) > 0 & gen(:, QG) < gen(:,
QMIN) );

        if ~isempty(mx) || ~isempty(mn)    %% we have some Q limit
violations
            if isempty(pv)
                if verbose
                    if ~isempty(mx)
                        fprintf('Gen %d (only one left) exceeds
upper Q limit : INFEASIBLE PROBLEM\n', mx);
                    else
                        fprintf('Gen %d (only one left) exceeds
lower Q limit : INFEASIBLE PROBLEM\n', mn);
                    end
                end
                success = 0;
                break;
            end

            %% one at a time?
            if qlim == 2    %% fix largest violation, ignore the
rest
                [junk, k] = max([gen(mx, QG) - gen(mx, QMAX);
                                gen(mn, QMIN) - gen(mn, QG)]);
                if k > length(mx)
                    mn = mn(k-length(mx));
                    mx = [];
                else
                    mx = mx(k);
                    mn = [];
                end
            end

            if verbose && ~isempty(mx)
                fprintf('Gen %d at upper Q limit, converting to PQ
bus\n', mx);
            end
            if verbose && ~isempty(mn)
                fprintf('Gen %d at lower Q limit, converting to PQ
bus\n', mn);
            end

            %% save corresponding limit values
            fixedQg(mx) = gen(mx, QMAX);

```

```

        fixedQg(mn) = gen(mn, QMIN);
        mx = [mx;mn];

        %% convert to PQ bus
        gen(mx, QG) = fixedQg(mx);          %% set Qg to binding
limit
        gen(mx, GEN_STATUS) = 0;            %% temporarily turn off
gen,
        for i = 1:length(mx)                %% (one at a time, since
            bi = gen(mx(i), GEN_BUS);      %% they may be at same
bus)
            bus(bi, [PD,QD]) = ...          %% adjust load
accordingly,
                bus(bi, [PD,QD]) - gen(mx(i), [PG,QG]);
        end
        bus(gen(mx, GEN_BUS), BUS_TYPE) = PQ; %% & set bus
type to PQ

        %% update bus index lists of each type of bus
        ref_temp = ref;
        [ref, pv, pq] = bustypes(bus, gen);
        if verbose && ref ~= ref_temp
            fprintf('Bus %d is new slack bus\n', ref);
        end
        limited = [limited; mx];
    else
        repeat = 0; %% no more generator Q limits violated
    end
else
    repeat = 0; %% don't enforce generator Q limits, once is
enough
end
end
if qlim && ~isempty(limited)
    %% restore injections from limited gens (those at Q limits)
    gen(limited, QG) = fixedQg(limited);    %% restore Qg value,
    for i = 1:length(limited)                %% (one at a time, since
        bi = gen(limited(i), GEN_BUS);      %% they may be at same
bus)
        bus(bi, [PD,QD]) = ...              %% re-adjust load,
            bus(bi, [PD,QD]) + gen(limited(i), [PG,QG]);
    end
    gen(limited, GEN_STATUS) = 1;            %% and turn gen back
on
    if ref ~= ref0
        %% adjust voltage angles to make original ref bus correct
        bus(:, VA) = bus(:, VA) - bus(ref0, VA) + Varef0;
    end
end
end
mpc.et = etime(clock, t0);
mpc.success = success;

%%----- output results -----
%% convert back to original bus numbering & print results
[mpc.bus, mpc.gen, mpc.branch] = deal(bus, gen, branch);
results = int2ext(mpc);

%% zero out result fields of out-of-service gens & branches
if ~isempty(results.order.gen.status.off)
    results.gen(results.order.gen.status.off, [PG QG]) = 0;
end
if ~isempty(results.order.branch.status.off)
    results.branch(results.order.branch.status.off, [PF QF PT QT]) = 0;
end

```

```

end

if fname
    [fd, msg] = fopen(fname, 'at');
    if fd == -1
        error(msg);
    else
        fprintf(results, fd, mpopt);
        fclose(fd);
    end
end
fprintf(results, 1, mpopt);

%% save solved case
if solvedcase
    savecase(solvedcase, results);
end

if nargout == 1 || nargout == 2
    MVABase = results;
    bus = success;
elseif nargout > 2
    [MVABase, bus, gen, branch, et] = ...
        deal(results.baseMVA, results.bus, results.gen, results.branch,
results.et);
% else %% don't define MVABase, so it doesn't print anything
end

```



# APPENDIX C-1

## POWER FLOW SIMULATION RESULTS FOR ORIGINAL LOAD (PD)

Newton's method power flow converged in 4 iterations.

Converged in 0.53 seconds

```
=====
=====
|      System Summary
|
=====
=====
```

How many? (MVar)		How much?	P (MW)	Q
-----		-----	-----	-----
Buses	24	Total Gen Capacity	3405.0	-535.0 to 1776.0
Generators	33	On-line Capacity	3405.0	-535.0 to 1776.0
Committed Gens	33	Generation (actual)	2901.2	587.4
Loads	17	Load	2850.0	580.0
Fixed	17	Fixed	2850.0	580.0
Dispatchable	0	Dispatchable	0.0 of 0.0	0.0
Shunts	1	Shunt (inj)	0.0	-102.5
Branches	38	Losses ( $I^2 \cdot Z$ )	51.25	454.77
Transformers	5	Branch Charging (inj)	-	549.9
Inter-ties	10	Total Inter-tie Flow	1339.8	204.9
Areas	4			

	Minimum	Maximum
-----	-----	-----
Voltage Magnitude	0.978 p.u. @ bus 24	1.050 p.u. @ bus 21
Voltage Angle	-12.42 deg @ bus 6	22.77 deg @ bus 22
P Losses ( $I^2 \cdot R$ )	-	7.05 MW @ line 14-16
Q Losses ( $I^2 \cdot X$ )	-	54.88 MVar @ line 14-16

```

=====
=====
|      Bus Data
|
=====
=====

```

Bus #	Voltage		Generation		Load	
	Mag(pu)	Ang(deg)	P (MW)	Q (MVar)	P (MW)	Q (MVar)
1	1.035	-7.278	172.00	21.47	108.00	22.00
2	1.035	-7.370	172.00	15.66	97.00	20.00
3	0.989	-5.584	-	-	180.00	37.00
4	0.998	-9.690	-	-	74.00	15.00
5	1.019	-9.964	-	-	71.00	14.00
6	1.012	-12.421	-	-	136.00	28.00
7	1.025	-7.357	240.00	51.84	125.00	25.00
8	0.993	-11.088	-	-	171.00	35.00
9	1.001	-7.435	-	-	175.00	36.00
10	1.028	-9.503	-	-	195.00	40.00
11	0.990	-2.154	-	-	-	-
12	1.003	-1.517	-	-	-	-
13	1.020	0.000	187.25	133.99	265.00	54.00
14	0.980	2.258	0.00	-27.72	194.00	39.00
15	1.014	11.566	215.00	-3.95	317.00	64.00
16	1.017	10.449	155.00	44.40	100.00	20.00
17	1.039	14.931	-	-	-	-
18	1.050	16.292	400.00	138.73	333.00	68.00
19	1.023	8.917	-	-	181.00	37.00
20	1.038	9.530	-	-	128.00	26.00
21	1.050	17.117	400.00	106.91	-	-
22	1.050	22.766	300.00	-29.55	-	-
23	1.050	10.572	660.00	135.59	-	-
24	0.978	5.299	-	-	-	-
Total:			2901.25	587.36	2850.00	580.00

```

=====
=====
|      Branch Data
|
=====
=====

```

Brnch * Z)	From #	To Bus	From Bus P (MW)	Injection Q (MVar)	To Bus P (MW)	Injection Q (MVar)	Loss (I^2 P (MW)	Q
(MVar)	-----	-----	-----	-----	-----	-----	-----	-
1	1	2	11.94	-26.92	-11.94	-22.45	0.004	
0.02								
2	1	3	-7.97	21.57	8.31	-26.11	0.342	
1.32								
3	1	5	60.03	4.83	-59.29	-4.37	0.741	
2.87								
4	2	4	38.44	19.15	-37.85	-20.43	0.587	
2.27								
5	2	6	48.50	-1.04	-47.41	-0.19	1.093	
4.22								
6	3	9	22.90	-17.01	-22.66	14.75	0.240	
0.93								
7	3	24	-211.21	6.12	212.32	34.48	1.113	
40.60								
8	4	9	-36.15	5.43	36.52	-6.83	0.364	
1.41								
9	5	10	-11.71	-9.63	11.76	7.30	0.046	
0.18								
10	6	10	-88.59	-130.31	89.66	-121.12	1.067	
4.64								
11	7	8	115.00	26.84	-112.88	-20.35	2.118	
8.18								
12	8	9	-36.92	3.36	37.53	-5.46	0.604	
2.34								
13	8	10	-21.19	-18.01	21.50	14.61	0.303	
1.17								
14	9	11	-105.92	-12.77	106.20	22.87	0.277	
10.10								
15	9	12	-120.47	-25.69	120.84	39.16	0.369	
13.47								
16	10	11	-151.18	36.03	151.72	-16.10	0.546	
19.93								
17	10	12	-166.74	23.18	167.38	0.21	0.641	
23.39								
18	11	13	-86.15	-54.97	86.76	49.70	0.618	
4.82								

19	11	14	-171.77	48.19	173.55	-42.96	1.778
13.76							
20	12	13	-60.51	-33.30	60.79	25.20	0.271
2.11							
21	12	23	-227.70	-6.07	234.10	34.52	6.399
49.85							
22	13	23	-225.30	5.10	230.74	17.80	5.438
42.38							
23	14	16	-367.55	-23.77	374.60	70.49	7.054
54.88							
24	15	16	112.30	-32.60	-112.01	31.13	0.290
2.28							
25	15	21	-214.92	-41.97	217.83	53.65	2.913
22.65							
26	15	21	-214.92	-41.97	217.83	53.65	2.913
22.65							
27	15	24	215.54	48.59	-212.32	-34.48	3.219
24.93							
28	16	17	-322.68	-33.86	326.03	54.42	3.353
26.31							
29	16	19	115.08	-43.35	-114.65	41.64	0.433
3.33							
30	17	18	-186.94	-58.69	187.58	60.49	0.638
5.10							
31	17	22	-139.09	4.28	141.54	-9.26	2.454
19.14							
32	18	21	-60.29	5.12	60.40	-10.26	0.111
0.87							
33	18	21	-60.29	5.12	60.40	-10.26	0.111
0.87							
34	19	20	-33.17	-39.32	33.29	31.34	0.113
0.88							
35	19	20	-33.17	-39.32	33.29	31.34	0.113
0.88							
36	20	23	-97.29	-44.34	97.58	41.63	0.291
2.25							
37	20	23	-97.29	-44.34	97.58	41.63	0.291
2.25							
38	21	22	-156.46	20.12	158.46	-20.29	1.994
15.54							
-----						-----	-
					Total:	51.246	454.77

## APPENDIX C-2

### POWER FLOW SIMULATION RESULTS FOR LOAD PD1 (PD+10%PD)

Newton's method power flow converged in 4 iterations.

Converged in 0.58 seconds

```
=====
=====
|      System Summary
|
=====
=====
```

How many? (MVar)		How much?	P (MW)	Q
-----		-----	-----	-----
Buses	24	Total Gen Capacity	3405.0	-535.0 to 1776.0
Generators	33	On-line Capacity	3405.0	-535.0 to 1776.0
Committed Gens	33	Generation (actual)	3185.7	610.6
Loads	17	Load	3135.0	580.0
Fixed	17	Fixed	3135.0	580.0
Dispatchable	0	Dispatchable	0.0 of 0.0	0.0
Shunts	1	Shunt (inj)	0.0	-101.3
Branches	38	Losses ( $I^2 * Z$ )	50.66	475.80
Transformers	5	Branch Charging (inj)	-	546.4
Inter-ties	10	Total Inter-tie Flow	1424.4	201.1
Areas	4			

	Minimum	Maximum
----	-----	-----
Voltage Magnitude	0.976 p.u. @ bus 24	1.050 p.u. @ bus 22
Voltage Angle	-17.51 deg @ bus 6	17.52 deg @ bus 22
P Losses ( $I^2 * R$ )	-	6.00 MW @ line 14-16
Q Losses ( $I^2 * X$ )	-	46.68 MVar @ line 14-16

=====						
Bus Data						
=====						
=====						
Bus	Voltage		Generation		Load	
#	Mag(pu)	Ang(deg)	P (MW)	Q (MVar)	P (MW)	Q (MVar)
-----						
1	1.035	-12.973	172.00	30.25	118.80	22.00
2	1.035	-13.056	172.00	24.00	106.70	20.00
3	0.985	-11.072	-	-	198.00	37.00
4	0.994	-14.874	-	-	81.40	15.00
5	1.015	-15.204	-	-	78.10	14.00
6	1.006	-17.507	-	-	149.60	28.00
7	1.025	-13.749	240.00	61.22	137.50	25.00
8	0.988	-16.976	-	-	188.10	35.00
9	0.997	-11.723	-	-	192.50	36.00
10	1.023	-13.903	-	-	214.50	40.00
11	0.986	-5.037	-	-	-	-
12	0.997	-3.908	-	-	-	-
13	1.020	0.000	471.66	122.83	291.50	54.00
14	0.980	-1.854	0.00	-23.03	213.40	39.00
15	1.014	6.367	215.00	3.02	348.70	64.00
16	1.017	5.654	155.00	39.41	110.00	20.00
17	1.039	9.766	-	-	-	-
18	1.050	10.939	400.00	140.90	366.30	68.00
19	1.023	4.727	-	-	199.10	37.00
20	1.038	6.041	-	-	140.80	26.00
21	1.050	11.823	400.00	106.49	-	-
22	1.050	17.522	300.00	-29.81	-	-
23	1.050	7.529	660.00	135.35	-	-
24	0.976	0.019	-	-	-	-
-----						
Total:			3185.66	610.62	3135.00	580.00
=====						
=====						
Branch Data						
=====						
=====						

Brnch * Z)	From	To	From Bus	Injection	To Bus	Injection	Loss (I <sup>2</sup>	
#	Bus	Bus	P (MW)	Q (MVar)	P (MW)	Q (MVar)	P (MW)	Q
(MVar)								
-----	-----	-----	-----	-----	-----	-----	-----	-
1	1	2	10.68	-26.69	-10.68	-22.69	0.003	
0.02								
2	1	3	-9.00	24.07	9.42	-28.29	0.416	
1.61								
3	1	5	51.52	10.88	-50.95	-11.07	0.570	
2.21								
4	2	4	32.36	23.63	-31.85	-25.15	0.519	
2.01								
5	2	6	43.61	3.07	-42.72	-5.01	0.898	
3.47								
6	3	9	6.40	-13.07	-6.34	10.12	0.055	
0.21								
7	3	24	-213.82	4.36	214.97	37.60	1.150	
41.97								
8	4	9	-49.55	10.15	50.26	-10.22	0.702	
2.72								
9	5	10	-27.15	-2.93	27.31	1.08	0.164	
0.63								
10	6	10	-106.88	-124.24	108.45	-122.06	1.568	
6.83								
11	7	8	102.50	36.22	-100.70	-30.96	1.798	
6.94								
12	8	9	-51.84	8.67	53.07	-8.34	1.226	
4.74								
13	8	10	-35.56	-12.72	36.16	10.52	0.601	
2.32								
14	9	11	-132.66	-9.30	133.09	25.14	0.434	
15.84								
15	9	12	-156.82	-18.26	157.44	40.59	0.612	
22.33								
16	10	11	-180.52	39.40	181.30	-10.91	0.781	
28.48								
17	10	12	-205.90	31.07	206.89	5.11	0.992	
36.17								
18	11	13	-190.36	-43.17	192.73	51.59	2.367	
18.47								

19	11	14	-124.03	28.95	124.95	-30.35	0.916
7.09							
20	12	13	-148.76	-29.77	150.15	30.51	1.397
10.90							
21	12	23	-215.57	-15.92	221.38	39.87	5.805
45.22							
22	13	23	-162.72	-13.28	165.55	15.83	2.826
22.03							
23	14	16	-338.35	-31.68	344.35	70.21	6.000
46.68							
24	15	16	70.81	-28.00	-70.69	25.20	0.122
0.96							
25	15	21	-211.40	-42.77	214.23	53.76	2.824
21.97							
26	15	21	-211.40	-42.77	214.23	53.76	2.824
21.97							
27	15	24	218.29	52.56	-214.97	-37.60	3.326
25.76							
28	16	17	-297.20	-39.94	300.06	56.64	2.862
22.46							
29	16	19	68.54	-36.06	-68.37	32.32	0.169
1.30							
30	17	18	-162.34	-60.76	162.84	61.44	0.498
3.98							
31	17	22	-137.72	4.12	140.12	-9.49	2.405
18.76							
32	18	21	-64.57	5.73	64.70	-10.74	0.127
1.00							
33	18	21	-64.57	5.73	64.70	-10.74	0.127
1.00							
34	19	20	-65.37	-34.66	65.62	27.78	0.253
1.97							
35	19	20	-65.37	-34.66	65.62	27.78	0.253
1.97							
36	20	23	-136.02	-40.78	136.54	39.83	0.519
4.00							
37	20	23	-136.02	-40.78	136.54	39.83	0.519
4.00							
38	21	22	-157.85	20.44	159.88	-20.33	2.029
15.81							
							----- -
Total:						50.660	475.80



# **APPENDIX C-3** **POWER FLOW SIMULATION RESULTS FOR PD2** **(PD1+10%PD1)**

Newton's method power flow converged in 4 iterations.

Converged in 0.03 seconds

```

=====
=====
|      System Summary
|
=====
=====

```

How many? (MVar)		How much?	P (MW)	Q
-----		-----	-----	-----
Buses	24	Total Gen Capacity	3405.0	-535.0 to 1776.0
Generators	33	On-line Capacity	3405.0	-535.0 to 1776.0
Committed Gens	33	Generation (actual)	3505.7	696.3
Loads	17	Load	3448.5	580.0
Fixed	17	Fixed	3448.5	580.0
Dispatchable	0	Dispatchable	0.0 of 0.0	0.0
Shunts	1	Shunt (inj)	0.0	-99.3
Branches	38	Losses (I <sup>2</sup> * Z)	57.15	557.76
Transformers	5	Branch Charging (inj)	-	540.7
Inter-ties	10	Total Inter-tie Flow	1518.4	211.1
Areas	4			

	Minimum	Maximum
-----	-----	-----
Voltage Magnitude	0.973 p.u. @ bus 24	1.050 p.u. @ bus 18
Voltage Angle	-23.78 deg @ bus 8	11.63 deg @ bus 22
P Losses (I <sup>2</sup> *R)	-	6.00 MW @ line 11-13
Q Losses (I <sup>2</sup> *X)	-	54.17 MVar @ line 10-12

```

=====
=====
|      Bus Data
|
=====
=====

```

Bus #	Voltage		Generation		Load	
	Mag (pu)	Ang (deg)	P (MW)	Q (MVar)	P (MW)	Q (MVar)
1	1.035	-19.541	172.00	43.29	130.68	22.00
2	1.035	-19.614	172.00	36.65	117.37	20.00
3	0.978	-17.337	-	-	217.80	37.00
4	0.988	-20.847	-	-	89.54	15.00
5	1.009	-21.249	-	-	85.91	14.00
6	0.996	-23.381	-	-	164.56	28.00
7	1.025	-21.136	240.00	75.01	151.25	25.00
8	0.982	-23.779	-	-	206.91	35.00
9	0.989	-16.640	-	-	211.75	36.00
10	1.013	-18.969	-	-	235.95	40.00
11	0.979	-8.307	-	-	-	-
12	0.987	-6.610	-	-	-	-
13	1.020	0.000	791.65	136.87	320.65	54.00
14	0.980	-6.504	0.00	-9.89	234.74	39.00
15	1.014	0.519	215.00	12.77	383.57	64.00
16	1.017	0.258	155.00	36.79	121.00	20.00
17	1.039	3.960	-	-	-	-
18	1.050	4.923	400.00	143.55	402.93	68.00
19	1.022	0.013	-	-	219.01	37.00
20	1.037	2.117	-	-	154.88	26.00
21	1.050	5.871	400.00	106.07	-	-
22	1.050	11.626	300.00	-30.08	-	-
23	1.050	4.105	660.00	145.31	-	-
24	0.973	-5.943	-	-	-	-
Total:			3505.65	696.33	3448.50	580.00

```

=====
=====
|      Branch Data
|
=====
=====

```

Brnch * Z)	From	To	From Bus	Injection	To Bus	Injection	Loss (I^2	
#	Bus	Bus	P (MW)	Q (MVar)	P (MW)	Q (MVar)	P (MW)	Q
(MVar)								
-----	-----	-----	-----	-----	-----	-----	-----	-
1	1	2	9.47	-26.46	-9.47	-22.92	0.002	
0.01								
2	1	3	-10.45	27.82	10.99	-31.53	0.542	
2.10								
3	1	5	42.30	19.93	-41.85	-20.56	0.455	
1.76								
4	2	4	25.69	30.35	-25.17	-31.85	0.519	
2.01								
5	2	6	38.40	9.22	-37.65	-11.69	0.751	
2.90								
6	3	9	-11.33	-7.15	11.38	4.24	0.051	
0.20								
7	3	24	-217.46	1.68	218.67	42.31	1.206	
43.99								
8	4	9	-64.37	16.85	65.59	-14.84	1.229	
4.76								
9	5	10	-44.06	6.56	44.51	-7.27	0.448	
1.74								
10	6	10	-126.91	-115.60	129.17	-122.86	2.261	
9.84								
11	7	8	88.75	50.01	-87.17	-45.57	1.584	
6.12								
12	8	9	-68.37	15.99	70.59	-11.76	2.217	
8.57								
13	8	10	-51.37	-5.43	52.55	5.52	1.174	
4.54								
14	9	11	-162.39	-5.09	163.05	29.13	0.659	
24.04								
15	9	12	-196.93	-8.54	197.90	43.92	0.970	
35.38								
16	10	11	-213.16	43.36	214.26	-3.12	1.103	
40.23								
17	10	12	-249.01	41.25	250.50	12.92	1.485	
54.17								
18	11	13	-306.03	-28.76	312.03	65.62	6.003	
46.84								

19	11	14	-71.28	2.76	71.57	-8.95	0.289
2.24							
20	12	13	-246.39	-27.36	250.22	47.20	3.832
29.90							
21	12	23	-202.01	-29.48	207.25	49.23	5.241
40.83							
22	13	23	-91.25	-29.95	92.19	17.74	0.933
7.27							
23	14	16	-306.31	-39.95	311.26	70.32	4.952
38.53							
24	15	16	24.50	-22.51	-24.48	18.93	0.022
0.17							
25	15	21	-207.61	-43.63	210.34	53.89	2.731
21.24							
26	15	21	-207.61	-43.63	210.34	53.89	2.731
21.24							
27	15	24	222.15	58.53	-218.67	-42.31	3.484
26.99							
28	16	17	-268.94	-46.38	271.30	59.21	2.368
18.59							
29	16	19	16.15	-26.08	-16.13	21.22	0.024
0.18							
30	17	18	-135.12	-63.13	135.49	62.76	0.367
2.94							
31	17	22	-136.19	3.92	138.54	-9.71	2.351
18.34							
32	18	21	-69.21	6.40	69.35	-11.26	0.146
1.15							
33	18	21	-69.21	6.40	69.35	-11.26	0.146
1.15							
34	19	20	-101.44	-29.11	101.97	24.41	0.533
4.13							
35	19	20	-101.44	-29.11	101.97	24.41	0.533
4.13							
36	20	23	-179.41	-37.41	180.28	39.17	0.870
6.71							
37	20	23	-179.41	-37.41	180.28	39.17	0.870
6.71							
38	21	22	-159.39	20.80	161.46	-20.37	2.070
16.13							
						-----	-
Total:						57.151	557.76

# **APPENDIX C-4** **POWER FLOW SIMULATION RESULTS FOR PD3** **(PD2+10%PD2)**

Newton's method power flow converged in 4 iterations.

Converged in 0.00 seconds

```

=====
=====
|      System Summary
|
=====
=====

```

How many? (MVar)		How much?	P (MW)	Q
-----		-----	-----	-----
Buses	24	Total Gen Capacity	3405.0	-535.0 to 1776.0
Generators	33	On-line Capacity	3405.0	-535.0 to 1776.0
Committed Gens	33	Generation (actual)	3867.7	874.9
Loads	17	Load	3793.3	580.0
Fixed	17	Fixed	3793.3	580.0
Dispatchable	0	Dispatchable	0.0 of 0.0	0.0
Shunts	1	Shunt (inj)	0.0	-96.3
Branches	38	Losses (I <sup>2</sup> * Z)	74.30	730.35
Transformers	5	Branch Charging (inj)	-	531.7
Inter-ties	10	Total Inter-tie Flow	1710.6	230.8
Areas	4			

	Minimum	Maximum
----	-----	-----
Voltage Magnitude	0.967 p.u. @ bus 11	1.050 p.u. @ bus 21
Voltage Angle	-31.86 deg @ bus 8	4.91 deg @ bus 22
P Losses (I <sup>2</sup> *R)	-	12.34 MW @ line 11-13
Q Losses (I <sup>2</sup> *X)	-	96.26 MVar @ line 11-13

```

=====
=====
|      Bus Data
|
=====
=====

```

Bus #	Voltage		Generation		Load	
	Mag (pu)	Ang (deg)	P (MW)	Q (MVar)	P (MW)	Q (MVar)
1	1.035	-27.314	172.00	62.70	143.75	22.00
2	1.035	-27.380	172.00	55.74	129.11	20.00
3	0.968	-24.648	-	-	239.58	37.00
4	0.977	-27.913	-	-	98.49	15.00
5	1.000	-28.412	-	-	94.50	14.00
6	0.981	-30.359	-	-	181.02	28.00
7	1.025	-29.914	240.00	95.39	166.38	25.00
8	0.971	-31.864	-	-	227.60	35.00
9	0.975	-22.421	-	-	232.93	36.00
10	0.997	-24.958	-	-	259.55	40.00
11	0.967	-12.089	-	-	-	-
12	0.972	-9.714	-	-	-	-
13	1.020	0.000	1153.65	188.67	352.71	54.00
14	0.980	-11.854	0.00	15.82	258.21	39.00
15	1.014	-6.153	215.00	26.67	421.93	64.00
16	1.017	-5.904	155.00	37.63	133.10	20.00
17	1.039	-2.658	-	-	-	-
18	1.050	-1.926	400.00	146.79	443.22	68.00
19	1.021	-5.364	-	-	240.91	37.00
20	1.036	-2.359	-	-	170.37	26.00
21	1.050	-0.910	400.00	105.67	-	-
22	1.050	4.909	300.00	-30.35	-	-
23	1.050	0.194	660.00	170.21	-	-
24	0.968	-12.787	-	-	-	-
Total:			3867.65	874.94	3793.35	580.00

```

=====
=====
|      Branch Data
|
=====
=====

```

Brnch * Z)	From	To	From Bus	Injection	To Bus	Injection	Loss (I <sup>2</sup>	
#	Bus	Bus	P (MW)	Q (MVar)	P (MW)	Q (MVar)	P (MW)	Q
(MVar)								
-----	-----	-----	-----	-----	-----	-----	-----	-
1	1	2	8.46	-26.27	-8.46	-23.11	0.002	
0.01								
2	1	3	-12.62	33.51	13.38	-36.30	0.763	
2.95								
3	1	5	32.41	33.47	-31.95	-34.06	0.459	
1.78								
4	2	4	18.37	40.42	-17.72	-41.38	0.650	
2.51								
5	2	6	32.98	18.44	-32.27	-20.97	0.714	
2.76								
6	3	9	-30.04	1.48	30.34	-3.36	0.299	
1.16								
7	3	24	-222.92	-2.18	224.22	49.38	1.294	
47.20								
8	4	9	-80.77	26.38	82.82	-21.14	2.045	
7.91								
9	5	10	-62.55	20.06	63.54	-18.59	0.995	
3.85								
10	6	10	-148.75	-103.29	151.98	-123.31	3.228	
14.05								
11	7	8	73.63	70.39	-72.04	-65.91	1.589	
6.14								
12	8	9	-86.78	26.19	90.54	-15.85	3.769	
14.57								
13	8	10	-68.79	4.71	70.95	-0.69	2.162	
8.36								
14	9	11	-195.56	0.05	196.54	35.78	0.982	
35.83								
15	9	12	-241.07	4.31	242.56	50.16	1.493	
54.46								
16	10	11	-249.62	48.05	251.17	8.65	1.555	
56.71								
17	10	12	-296.40	54.53	298.59	25.18	2.185	
79.71								
18	11	13	-434.67	-11.27	447.00	97.67	12.336	
96.26								

19	11	14	-13.04	-33.16	13.10	25.29	0.059
0.45							
20	12	13	-354.38	-27.14	362.52	80.72	8.138
63.50							
21	12	23	-186.77	-48.19	191.54	64.59	4.772
37.18							
22	13	23	-8.58	-43.72	8.71	25.28	0.133
1.04							
23	14	16	-271.32	-48.46	275.25	70.93	3.936
30.62							
24	15	16	-27.69	-15.88	27.71	12.29	0.021
0.16							
25	15	21	-203.59	-44.53	206.23	54.04	2.634
20.49							
26	15	21	-203.59	-44.53	206.23	54.04	2.634
20.49							
27	15	24	227.95	67.60	-224.22	-49.38	3.735
28.93							
28	16	17	-237.45	-53.19	239.33	62.18	1.880
14.75							
29	16	19	-43.61	-12.39	43.67	7.80	0.058
0.45							
30	17	18	-104.87	-65.85	105.12	64.56	0.252
2.02							
31	17	22	-134.46	3.66	136.75	-9.93	2.290
17.87							
32	18	21	-74.17	7.12	74.34	-11.81	0.168
1.32							
33	18	21	-74.17	7.12	74.34	-11.81	0.168
1.32							
34	19	20	-142.29	-22.40	143.30	21.41	1.007
7.82							
35	19	20	-142.29	-22.40	143.30	21.41	1.007
7.82							
36	20	23	-228.48	-34.41	229.87	40.17	1.388
10.71							
37	20	23	-228.48	-34.41	229.87	40.17	1.388
10.71							
38	21	22	-161.14	21.21	163.25	-20.42	2.116
16.49							
-----						-----	-
					Total:	74.304	730.35



# **APPENDIX C-5** **POWER FLOW SIMULATION RESULTS FOR PD4** **(PD3+10%PD3)**

Newton's method power flow converged in 5 iterations.

Converged in 0.02 seconds

```

=====
=====
|      System Summary
|
=====
=====

```

How many? (MVar)		How much?	P (MW)	Q
-----		-----	-----	-----
Buses	24	Total Gen Capacity	3405.0	-535.0 to 1776.0
Generators	33	On-line Capacity	3405.0	-535.0 to 1776.0
Committed Gens	33	Generation (actual)	4281.4	1202.0
Loads	17	Load	4172.7	580.0
Fixed	17	Fixed	4172.7	580.0
Dispatchable	0	Dispatchable	0.0 of 0.0	0.0
Shunts	1	Shunt (inj)	0.0	-91.5
Branches	38	Losses (I <sup>2</sup> * Z)	108.72	1047.74
Transformers	5	Branch Charging (inj)	-	517.2
Inter-ties	10	Total Inter-tie Flow	1968.5	274.7
Areas	4			

	Minimum	Maximum
-----	-----	-----
Voltage Magnitude	0.947 p.u. @ bus 11	1.050 p.u. @ bus 18
Voltage Angle	-41.97 deg @ bus 8	0.00 deg @ bus 13
P Losses (I <sup>2</sup> *R)	-	22.75 MW @ line 11-13
Q Losses (I <sup>2</sup> *X)	-	177.53 MVar @ line 11-13

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|      Bus Data
|
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```

Bus #	Voltage		Generation		Load	
	Mag(pu)	Ang(deg)	P (MW)	Q (MVar)	P (MW)	Q (MVar)
1	1.035	-36.952	172.00	92.63	158.12	22.00
2	1.035	-37.014	172.00	85.47	142.02	20.00
3	0.952	-33.518	-	-	263.54	37.00
4	0.961	-36.677	-	-	108.34	15.00
5	0.985	-37.319	-	-	103.95	14.00
6	0.957	-39.065	-	-	199.12	28.00
7	1.025	-40.872	240.00	126.61	183.01	25.00
8	0.955	-41.966	-	-	250.36	35.00
9	0.951	-29.520	-	-	256.22	36.00
10	0.971	-32.382	-	-	285.50	40.00
11	0.947	-16.607	-	-	-	-
12	0.948	-13.382	-	-	-	-
13	1.020	0.000	1567.40	300.59	387.99	54.00
14	0.980	-18.192	0.00	61.73	284.04	39.00
15	1.014	-13.954	215.00	47.48	464.12	64.00
16	1.017	-13.118	155.00	43.70	146.41	20.00
17	1.039	-10.383	-	-	-	-
18	1.050	-9.910	400.00	150.72	487.54	68.00
19	1.019	-11.652	-	-	265.00	37.00
20	1.034	-7.596	-	-	187.40	26.00
21	1.050	-8.823	400.00	105.32	-	-
22	1.050	-2.931	300.00	-30.61	-	-
23	1.050	-4.391	660.00	218.39	-	-
24	0.960	-20.876	-	-	-	-
Total:			4281.40	1202.03	4172.68	580.00

```

=====
=====
|      Branch Data
|
=====
=====

```

Brnch * Z)	From	To	From Bus Injection	To Bus Injection	Loss (I^2
#	Bus	Bus	P (MW)	Q (MVar)	P (MW)
(MVar)					
-----	-----	-----	-----	-----	-----
-----					
1	1	2	8.01	-26.19	-8.01
0.01					-23.20
					0.002
2	1	3	-16.18	42.48	17.37
4.61					-43.53
					1.191
3	1	5	22.05	54.34	-21.32
2.82					-53.86
					0.727
4	2	4	10.34	55.97	-9.29
4.08					-55.31
					1.056
5	2	6	27.64	32.69	-26.70
3.63					-34.23
					0.938
6	3	9	-49.06	14.05	49.95
3.47					-13.50
					0.899
7	3	24	-231.85	-7.52	233.30
52.82					60.34
					1.448
8	4	9	-99.05	40.31	102.40
12.96					-29.92
					3.350
9	5	10	-82.63	39.86	84.62
7.74					-34.40
					2.000
10	6	10	-172.42	-85.26	177.05
20.15					-122.99
					4.629
11	7	8	56.99	101.61	-54.91
8.04					-95.20
					2.081
12	8	9	-107.46	40.90	113.73
24.24					-20.72
					6.270
13	8	10	-87.99	19.30	91.83
14.84					-8.60
					3.839
14	9	11	-232.82	6.44	234.28
53.38					46.93
					1.463
15	9	12	-289.49	21.69	291.76
82.92					61.23
					2.273
16	10	11	-290.72	53.69	292.94
80.92					27.23
					2.218
17	10	12	-348.28	72.31	351.49
117.15					44.85
					3.212
18	11	13	-578.36	9.63	601.11
177.53					158.22
					22.751

19	11	14	51.14	-83.80	-50.59	79.82	0.541
4.19							
20	12	13	-473.77	-31.50	489.04	141.02	15.276
119.20							
21	12	23	-169.49	-74.57	174.04	89.71	4.552
35.46							
22	13	23	89.26	-52.65	-88.21	41.35	1.049
8.17							
23	14	16	-233.45	-57.09	236.43	72.15	2.984
23.22							
24	15	16	-87.64	-7.68	87.81	5.22	0.165
1.30							
25	15	21	-199.48	-45.44	202.01	54.20	2.537
19.73							
26	15	21	-199.48	-45.44	202.01	54.20	2.537
19.73							
27	15	24	237.48	82.04	-233.30	-60.34	4.176
32.34							
28	16	17	-202.09	-60.38	203.50	65.68	1.409
11.06							
29	16	19	-113.56	6.71	113.94	-8.83	0.377
2.90							
30	17	18	-71.03	-69.00	71.19	66.97	0.160
1.28							
31	17	22	-132.47	3.33	134.69	-10.14	2.222
17.33							
32	18	21	-79.36	7.87	79.56	-12.37	0.192
1.51							
33	18	21	-79.36	7.87	79.56	-12.37	0.192
1.51							
34	19	20	-189.47	-14.08	191.24	19.04	1.769
13.74							
35	19	20	-189.47	-14.08	191.24	19.04	1.769
13.74							
36	20	23	-284.94	-32.04	287.08	43.67	2.147
16.56							
37	20	23	-284.94	-32.04	287.08	43.67	2.147
16.56							
38	21	22	-163.14	21.67	165.31	-20.47	2.169
16.90							
						-----	-
Total:						108.716	1047.74

## APPENDIX D

### TRANSMISSION LOSS ALGORITHMS

```

%*****PRO RATA
generators*****
%Pg=total active power generated
%Pd=total active power demand
%Pgi=power output of generators of bus i
%L=transmission power losses
%Lgi=losses allocated to generator i
%Lgi=(L/2)*(Pgi/Pg)
%Generators are at bus [1 2 7 13 15 16 18 21 22 23]

%calculating the losses

Pgi = [172 172 240 187.25 215 155 400 400 300 660];
Pd = 2850;
Pg=2901.25;
L = Pg-Pd;
Lgi=(L/2)*(Pgi/Pg)

%*****PRO RATA LOADS*****8

%Pg=total active power generated
%Pd=total active power demand
%Pgi=power output of generators of bus i
%L=transmission power losses
%Lgi=losses allocated to generator i
%Lgi=(L/2)*(Pgi/Pg)
%Generators are at bus [1 2 7 13 15 16 18 21 22 23]

%calculating the losses

Pd = [108 97 180 74 71 136 125 171 175 195 266 194 317 100 333 181
128];
Pd = 2850;
Pg=2901.25;
L = Pg-Pd;
Ldj=(L/2)*(Pd/Pd)

%*****INCREMENTAL
ALLOCATION (ITL) generator*****

%Ploss=system transmission losses
%Pi is power injection at individual loads
%Ki=ITL corresponding to bus i
%Lgi_final=losses allocated to each genear
Pgi = [172 172 240 187.25 215 155 400 400 300 660];

Pdi = [108 97 125 265 317 100 333 0 0 0 ];
L=51.52;

%calculating Ki
Pi=Pgi-Pdi;
Ki=L./Pi;

Lgi3=Pgi.*Ki;
L_sum=sum(Lgi3);

```

```

Ki_new = Ki.*(L./L_sum);
Lgi_final = Pgi.*Ki_new

%Ploss_total = 51.52; %taken from pf solution
%Pi=[108 97 125 265 317 100 333 0 0 0];

%Ploss=Ploss_total./Pi

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%ITL loads%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%8

%Ploss=system transmission losses
%Pi is power injection at individual loads
%Ki=ITL corresponding to bus i
%Lgi_final=losses allocated to each generator

Pdj = [108 97 180 74 71 136 125 171 175 195 265 194 317 100 333 181
128];
Pd = 2850;

PgiL = [172 172 0 0 0 0 240 0 0 0 187.25 0 215 155 400 0 0];

L=51.52;

%calculating Ki
Pi=PgiL-Pdj;
Ki=L./Pi;

Ldj2=PgiL.*Ki;
L_sum=sum(Ldj2);
Ki_new = Ki.*(L./L_sum)
Ldj2_final = Pdj.*Ki_new;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Unsubdised
ITL(generators) %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pgi = [172 172 240 187.25 215 155 400 400 300 660];
Ki_new = [0.0561 0.0479 0.0312 -0.0462 -0.0352 0.0653 0.0536 0.0090
0.0120 0.0054]
Kgk = -0.0462;

Bg = 1/(1-Kgk);

Kgi = Bg.*Ki_new + (1-Bg);

Lgi4 = Kgi.* Pgi

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Unsubdised
ITL(loads) %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pdj = [108 97 180 74 71 136 125 171 175 195 265 194 317 100 333 181
128];
Ki_new =[0.0710 0.0606 -0.0252 -0.0614 -0.0640 -0.0334 0.0395 -0.0266 -
0.0260 -0.0233 -0.0584 -0.0234 -0.0445 0.0826 0.0678 -0.0251 -0.0355]
Kgk = 0.0826;

Bd = 1/(1-Kgk);

Kdi = Bd.*Ki_new + (1-Bd);

```

```

Ldj4 = -Kdi.* Pdj

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%PS generator%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pin= [64 86.94 -58.11 -207.6 -225.3 -102 -207.6 -156.46 0 0];
%calculated in the load flow
Pout= [-62.92 -85.26 -112.88 230.74 111.33 211.38 120.8 0 0];
LossG=(Pin+Pout)/2

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%PS loads%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pin= [64 86.94 -188.31 -36.15 -11.71 -88.59 115 -58.11 -226.39 -317.92 -
225.30 -367.55 -102 -207.6 -120.58 -66.34 -194.58]; %calculated in the
load flow
Pout= [-62.92 -85.26 189.66 36.52 11.76 89.66 -112.88 59.03 229.2 319.1
230.74 374.6 111.33 211.38 120.8 66.58 195.16];%calculated in the load
flow

LossL=(Pin+Pout)/2

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Plot
generators%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
PR_G = [1.5192 1.5192 2.1198 1.6539 1.899 1.369 3.533 3.533 2.6497
5.8294];
PS_G = [1.0800 1.6800 2.1200 5.4400 9.3300 3.7800
0.2200 2.0000 0 0];
BusG = [1 2 7 13 15 16 18 21 22 23];
ITL_G = [9.6556 8.2394 7.4980 -8.6527 -7.5730 10.1251 21.4494 3.5928
3.5928 3.5928];
UITL_G = [16.8186 15.4705 17.7557 0.0000 2.2606 16.5193 38.1571 21.1050
16.6890 32.5521];

figure(1)
plot(BusG,PR_G,'blue')
title('Losses allocated to generators (MW)')
xlabel('Bus')
ylabel('Losses (MW)')

hold on
plot(BusG,PS_G,'red')

hold on
plot(BusG,ITL_G,'yellow')

hold on
plot(BusG,UITL_G,'green')

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%PLOT LOADS%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

BusL = [1 2 3 4 5 6 7 8 9 10 13 14 15 16 18 19 20];
PR_L = [0.9711 0.8721 1.6184 0.6654 0.6384 1.2228 1.1239 1.5375 1.5735
1.7533 2.3917 1.7443 2.8502 0.8991 2.9941 1.6274 1.1509];
PS_L = [0.5400 0.8400 0.6750 0.1850 0.0250 0.5350 1.0600 0.4600 1.4050
0.5900 2.7200 3.5250 4.6650 1.8900 0.1100 0.1200 0.2900];
ITL_L = [7.6667 5.8759 -4.5432 -4.5432 -4.5432 -4.5432 4.9383 -4.5432 -
4.5432 -4.5432 -15.4850 -4.5432 -14.1197 8.2604 22.5806 -4.5432 -
4.5432];

```

```

UITL_L = [1.3656 2.3261 21.1511 11.6154 11.3458 17.1964 5.8726 20.3545
20.7162 22.5098 40.7292 22.4155 43.9184 0.0000 5.3721 21.2489 16.4779];

figure(2)
plot(BusL, PR_L, 'blue')
title('Losses allocated to loads (MW)')
xlabel('Bus')
ylabel('Losses (MW)')

hold on
plot(BusL, PS_L, 'red')

hold on
plot(BusL, ITL_L, 'yellow')

hold on
plot(BusL, UITL_L, 'green')

%*****correlation*****

figure(3)
crosscorr(PS_L, PR_L)
title('PS_L&PR_L')

figure(4)
crosscorr(PS_L, ITL_L)
title('PS_L&ITL_L')

figure(5)
crosscorr(PS_L, UITL_L)
title('PS_L&UITL_L')

figure(6)
crosscorr(PR_L, ITL_L)
title('PR_L&ITL_L')

figure(7)
crosscorr(PR_L, UITL_L)
title('PR_L&UITL_L')

figure(8)
crosscorr(ITL_L, UITL_L)
title('ITL_L&UITL_L')

```



# APPENDIX E

## PREDICTION USING MATLAB

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 1%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=1.188;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.00989;
Losst2 = 0.00999;
Losst3 = 0.01224;
%Losst4 = 0.0192;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 2%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=1.067;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.01417;
Losst2 = 0.0127;
Losst3 = 0.01364;
%Losst4 = 0.01994;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 3%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=1.98;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.01205;
Losst2 = 0.01257;
Losst3 = 0.01593;
%Losst4 = 0.02347;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 4%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
Pd1=0.814;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.0072;
Losst2 = 0.01229;
Losst3 = 0.02045;
%Losst4 = 0.0335;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 5%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
Pd1=0.781;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.00164;
Losst2 = 0.00448;
Losst3 = 0.0095;
%Losst4 = 0.02;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 6%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
Pd1=1.496;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.01568;
Losst2 = 0.02261;
Losst3 = 0.03228;
%Losst4 = 0.04629;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

%%Bus 7%%

```
Pd1=1.375;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.01798;
Losst2 = 0.01584;
Losst3 = 0.01589;
%Losst4 = 0.02081;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

%%Bus 8%%

```
Pd1=1.881;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.01827;
Losst2 = 0.03391;
Losst3 = 0.05931;
%Losst4 = 0.10109;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

%%Bus 9%%

```
Pd1=1.925;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
```

```
Losst1 = 0.01046;
Losst2 = 0.01629;
Losst3 = 0.02475;
%Losst4 = 0.03736;
```

```
A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
```

```
Coeff = inv(A)*B
```

```
Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4
```

%%Bus10%%

```
Pd1=2.145;
```

```

Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.01773;
Losst2 = 0.02588;
Losst3 = 0.0374;
%Losst4 = 0.0543;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus13%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=2.915;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.02826;
Losst2 = 0.00933;
Losst3 = 0.00133;
%Losst4 = 0.01049;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus14%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=2.134;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.06;
Losst2 = 0.04952;
Losst3 = 0.03936;
%Losst4 = 0.02984;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 15%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=3.487;
Pd2=Pd1*0.1+Pd1;

```

```

Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;
Losst1 = 0.09096;
Losst2 = 0.08968;
Losst3 = 0.09024;
%Losst4 = 0.09415;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus16%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=1.10;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.03031;
Losst2 = 0.02392;
Losst3 = 0.01938;
%Losst4 = 0.01786;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus18%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=3.663;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.00254;
Losst2 = 0.00292;
Losst3 = 0.00336;
%Losst4 = 0.00384;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus19%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

Pd1=1.991;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

```

```

Losst1 = 0.00506;
Losst2 = 0.01066;
Losst3 = 0.02014;
%Losst4 = 0.03538;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Bus 20%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
Pd1=1.408;
Pd2=Pd1*0.1+Pd1;
Pd3=Pd2*0.1+Pd2;
Pd4=Pd3*0.1+Pd3;

Losst1 = 0.01038;
Losst2 = 0.0174;
Losst3 = 0.02776;
%Losst4 = 0.04294;

A = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];
B = [Losst1;Losst2;Losst3];
C = [1/Pd1 1 Pd1;1/Pd2 1 Pd2;1/Pd3 1 Pd3];

Coeff = inv(A)*B

Losst4 = Coeff(1,1)/Pd4 + Coeff(2,1) + Coeff(3,1)*Pd4

```